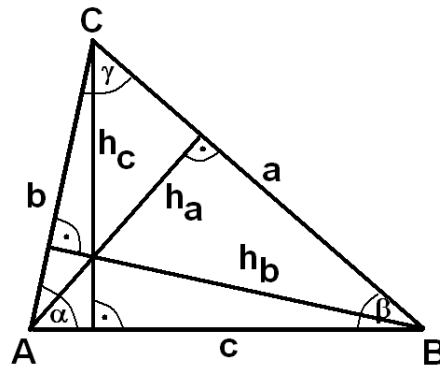


# Mathematik-Aufgabenpool

## > Berechnungen in allgemeinen Dreiecken II

**Einleitung:** In einem allgemeinen Dreieck  $\triangle ABC$  mit den Seiten  $a, b, c$  und den Höhen  $h_a, h_b, h_c$  lassen sich Umfang und Flächeninhalt des Dreiecks berechnen als:  $u = a + b + c$ ,  $A = ah_a/2 = bh_b/2 = ch_c/2$ . Umstellen der Flächenformel führt auf die Berechnung von Dreiecksseiten bzw. -höhen.



**Allgemeines Dreieck:** Seiten  $a, b, c$ ; Höhen  $h_a, h_b, h_c$

**Formelsammlung:**

Umfang	$u = a + b + c$		
Flächeninhalt	$A = \frac{1}{2}ah_a$	$A = \frac{1}{2}bh_b$	$A = \frac{1}{2}ch_c$
Seiten	$a = \frac{2A}{h_a}$	$b = \frac{2A}{h_b}$	$c = \frac{2A}{h_c}$
Höhen	$h_a = \frac{2A}{a}$	$h_b = \frac{2A}{b}$	$h_c = \frac{2A}{c}$

**Aufgabe 1:** Berechne Umfang und Flächeninhalt des allgemeinen Dreiecks (Seiten  $a, b, c$ , Höhen  $h_a, h_b, h_c$ ,  $u =$  Umfang,  $A =$  Flächeninhalt).

Nr.	Gegeben:
1	$a = 7.1 \text{ cm}, b = 9.2 \text{ cm}, c = 13.7 \text{ cm}, h_b = 6.5 \text{ cm}$
2	$a = 3 \text{ cm}, b = 2.1 \text{ cm}, c = 4.5 \text{ cm}, h_c = 1.2 \text{ cm}$
3	$a = 8.8 \text{ cm}, b = 4.9 \text{ cm}, c = 8.6 \text{ cm}, h_c = 4.8 \text{ cm}$
4	$a = 3.1 \text{ cm}, b = 6.2 \text{ cm}, c = 4.9 \text{ cm}, h_c = 3.1 \text{ cm}$
5	$a = 8.2 \text{ cm}, b = 6.8 \text{ cm}, c = 12.7 \text{ cm}, h_a = 6.1 \text{ cm}$
6	$a = 1.4 \text{ cm}, b = 1.2 \text{ cm}, c = 1.7 \text{ cm}, h_a = 1.2 \text{ cm}$
7	$a = 8.4 \text{ cm}, b = 7.3 \text{ cm}, c = 15.1 \text{ cm}, h_b = 4.4 \text{ cm}$
8	$a = 1.4 \text{ cm}, b = 7.6 \text{ cm}, c = 7.6 \text{ cm}, h_c = 1.4 \text{ cm}$
9	$a = 2.6 \text{ cm}, b = 7.1 \text{ cm}, c = 4.8 \text{ cm}, h_c = 1.5 \text{ cm}$
10	$a = 2.4 \text{ cm}, b = 3 \text{ cm}, c = 3.5 \text{ cm}, h_b = 2.4 \text{ cm}$

11	$a = 5.5 \text{ cm}, b = 7.1 \text{ cm}, c = 6.3 \text{ cm}, h_a = 6 \text{ cm}$
12	$a = 1.9 \text{ cm}, b = 2.8 \text{ cm}, c = 1.7 \text{ cm}, h_c = 1.9 \text{ cm}$
13	$a = 8.7 \text{ cm}, b = 6.5 \text{ cm}, c = 12.8 \text{ cm}, h_a = 5.9 \text{ cm}$
14	$a = 3.3 \text{ cm}, b = 9.9 \text{ cm}, c = 10.2 \text{ cm}, h_a = 9.9 \text{ cm}$
15	$a = 2.4 \text{ cm}, b = 2.6 \text{ cm}, c = 4.1 \text{ cm}, h_c = 1.4 \text{ cm}$
16	$a = 1.5 \text{ cm}, b = 1.1 \text{ cm}, c = 1.1 \text{ cm}, h_a = 0.8 \text{ cm}$
17	$a = 8.5 \text{ cm}, b = 1.2 \text{ cm}, c = 8.2 \text{ cm}, h_c = 1.2 \text{ cm}$
18	$a = 4.8 \text{ cm}, b = 7.4 \text{ cm}, c = 6.2 \text{ cm}, h_a = 6.2 \text{ cm}$
19	$a = 2.2 \text{ cm}, b = 5.9 \text{ cm}, c = 8 \text{ cm}, h_a = 2 \text{ cm}$
20	$a = 8 \text{ cm}, b = 5.2 \text{ cm}, c = 9.4 \text{ cm}, h_b = 8 \text{ cm}$

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	$a = 7.1 \text{ cm}, b = 9.2 \text{ cm}, c = 13.7 \text{ cm}, h_b = 6.5 \text{ cm}$	$u = 30 \text{ cm}, A = 29.9 \text{ cm}^2$
2	$a = 3 \text{ cm}, b = 2.1 \text{ cm}, c = 4.5 \text{ cm}, h_c = 1.2 \text{ cm}$	$u = 9.6 \text{ cm}, A = 2.6 \text{ cm}^2$
3	$a = 8.8 \text{ cm}, b = 4.9 \text{ cm}, c = 8.6 \text{ cm}, h_c = 4.8 \text{ cm}$	$u = 22.3 \text{ cm}, A = 20.4 \text{ cm}^2$
4	$a = 3.1 \text{ cm}, b = 6.2 \text{ cm}, c = 4.9 \text{ cm}, h_c = 3.1 \text{ cm}$	$u = 14.2 \text{ cm}, A = 7.5 \text{ cm}^2$
5	$a = 8.2 \text{ cm}, b = 6.8 \text{ cm}, c = 12.7 \text{ cm}, h_a = 6.1 \text{ cm}$	$u = 27.7 \text{ cm}, A = 25.2 \text{ cm}^2$
6	$a = 1.4 \text{ cm}, b = 1.2 \text{ cm}, c = 1.7 \text{ cm}, h_a = 1.2 \text{ cm}$	$u = 4.3 \text{ cm}, A = 0.8 \text{ cm}^2$
7	$a = 8.4 \text{ cm}, b = 7.3 \text{ cm}, c = 15.1 \text{ cm}, h_b = 4.4 \text{ cm}$	$u = 30.8 \text{ cm}, A = 16.2 \text{ cm}^2$
8	$a = 1.4 \text{ cm}, b = 7.6 \text{ cm}, c = 7.6 \text{ cm}, h_c = 1.4 \text{ cm}$	$u = 16.6 \text{ cm}, A = 5.3 \text{ cm}^2$
9	$a = 2.6 \text{ cm}, b = 7.1 \text{ cm}, c = 4.8 \text{ cm}, h_c = 1.5 \text{ cm}$	$u = 14.5 \text{ cm}, A = 3.5 \text{ cm}^2$
10	$a = 2.4 \text{ cm}, b = 3 \text{ cm}, c = 3.5 \text{ cm}, h_b = 2.4 \text{ cm}$	$u = 8.9 \text{ cm}, A = 3.5 \text{ cm}^2$
11	$a = 5.5 \text{ cm}, b = 7.1 \text{ cm}, c = 6.3 \text{ cm}, h_a = 6 \text{ cm}$	$u = 18.9 \text{ cm}, A = 16.6 \text{ cm}^2$
12	$a = 1.9 \text{ cm}, b = 2.8 \text{ cm}, c = 1.7 \text{ cm}, h_c = 1.9 \text{ cm}$	$u = 6.4 \text{ cm}, A = 1.6 \text{ cm}^2$
13	$a = 8.7 \text{ cm}, b = 6.5 \text{ cm}, c = 12.8 \text{ cm}, h_a = 5.9 \text{ cm}$	$u = 28 \text{ cm}, A = 25.8 \text{ cm}^2$
14	$a = 3.3 \text{ cm}, b = 9.9 \text{ cm}, c = 10.2 \text{ cm}, h_a = 9.9 \text{ cm}$	$u = 23.4 \text{ cm}, A = 16.3 \text{ cm}^2$
15	$a = 2.4 \text{ cm}, b = 2.6 \text{ cm}, c = 4.1 \text{ cm}, h_c = 1.4 \text{ cm}$	$u = 9.1 \text{ cm}, A = 2.9 \text{ cm}^2$
16	$a = 1.5 \text{ cm}, b = 1.1 \text{ cm}, c = 1.1 \text{ cm}, h_a = 0.8 \text{ cm}$	$u = 3.7 \text{ cm}, A = 0.6 \text{ cm}^2$
17	$a = 8.5 \text{ cm}, b = 1.2 \text{ cm}, c = 8.2 \text{ cm}, h_c = 1.2 \text{ cm}$	$u = 17.9 \text{ cm}, A = 4.8 \text{ cm}^2$
18	$a = 4.8 \text{ cm}, b = 7.4 \text{ cm}, c = 6.2 \text{ cm}, h_a = 6.2 \text{ cm}$	$u = 18.4 \text{ cm}, A = 14.8 \text{ cm}^2$
19	$a = 2.2 \text{ cm}, b = 5.9 \text{ cm}, c = 8 \text{ cm}, h_a = 2 \text{ cm}$	$u = 16.1 \text{ cm}, A = 2.2 \text{ cm}^2$
20	$a = 8 \text{ cm}, b = 5.2 \text{ cm}, c = 9.4 \text{ cm}, h_b = 8 \text{ cm}$	$u = 22.6 \text{ cm}, A = 20.8 \text{ cm}^2$

**Aufgabe 2:** Berechne Umfang und Flächeninhalt des allgemeinen Dreiecks (Seiten  $a, b, c$ , Höhen  $h_a, h_b, h_c$ ,  $u$  = Umfang,  $A$  = Flächeninhalt).

Nr.	Gegeben:
1	$a = 18 \text{ cm}, b = 19.9 \text{ cm}, c = 27.8 \text{ cm}, h_b = 18 \text{ cm}$
2	$a = 13.7 \text{ cm}, b = 9.9 \text{ cm}, c = 21.3 \text{ cm}, h_c = 5 \text{ cm}$
3	$a = 18.5 \text{ cm}, b = 13.6 \text{ cm}, c = 10.7 \text{ cm}, h_c = 13.5 \text{ cm}$
4	$a = 13.5 \text{ cm}, b = 8.5 \text{ cm}, c = 19.7 \text{ cm}, h_a = 6.9 \text{ cm}$

5	$a = 11.7 \text{ cm}, b = 17.3 \text{ cm}, c = 25.5 \text{ cm}, h_a = 14.7 \text{ cm}$
6	$a = 5.1 \text{ cm}, b = 18.1 \text{ cm}, c = 13.9 \text{ cm}, h_c = 3.3 \text{ cm}$
7	$a = 15.7 \text{ cm}, b = 14.3 \text{ cm}, c = 28.7 \text{ cm}, h_b = 8.8 \text{ cm}$
8	$a = 19.8 \text{ cm}, b = 6.8 \text{ cm}, c = 22 \text{ cm}, h_b = 19.5 \text{ cm}$
9	$a = 15 \text{ cm}, b = 19.3 \text{ cm}, c = 6.3 \text{ cm}, h_b = 4 \text{ cm}$
10	$a = 19 \text{ cm}, b = 15.1 \text{ cm}, c = 29.7 \text{ cm}, h_c = 8.3 \text{ cm}$
11	$a = 12.1 \text{ cm}, b = 18.7 \text{ cm}, c = 10.1 \text{ cm}, h_b = 5.9 \text{ cm}$
12	$a = 7.3 \text{ cm}, b = 15 \text{ cm}, c = 10.9 \text{ cm}, h_a = 10.3 \text{ cm}$
13	$a = 12.2 \text{ cm}, b = 8.8 \text{ cm}, c = 11.1 \text{ cm}, h_a = 7.7 \text{ cm}$
14	$a = 14.6 \text{ cm}, b = 11.4 \text{ cm}, c = 14 \text{ cm}, h_c = 10.7 \text{ cm}$
15	$a = 17.1 \text{ cm}, b = 6.3 \text{ cm}, c = 12 \text{ cm}, h_a = 3.1 \text{ cm}$
16	$a = 18.1 \text{ cm}, b = 12 \text{ cm}, c = 26.4 \text{ cm}, h_b = 15.5 \text{ cm}$
17	$a = 7.6 \text{ cm}, b = 10.5 \text{ cm}, c = 13.4 \text{ cm}, h_a = 10.5 \text{ cm}$
18	$a = 7.7 \text{ cm}, b = 5.6 \text{ cm}, c = 8.8 \text{ cm}, h_c = 4.8 \text{ cm}$
19	$a = 10.8 \text{ cm}, b = 12.8 \text{ cm}, c = 11.7 \text{ cm}, h_c = 10.1 \text{ cm}$
20	$a = 17.8 \text{ cm}, b = 6.6 \text{ cm}, c = 12.5 \text{ cm}, h_b = 8.8 \text{ cm}$

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	$a = 18 \text{ cm}, b = 19.9 \text{ cm}, c = 27.8 \text{ cm}, h_b = 18 \text{ cm}$	$u = 65.7 \text{ cm}, A = 178.6 \text{ cm}^2$
2	$a = 13.7 \text{ cm}, b = 9.9 \text{ cm}, c = 21.3 \text{ cm}, h_c = 5 \text{ cm}$	$u = 44.9 \text{ cm}, A = 53.2 \text{ cm}^2$
3	$a = 18.5 \text{ cm}, b = 13.6 \text{ cm}, c = 10.7 \text{ cm}, h_c = 13.5 \text{ cm}$	$u = 42.8 \text{ cm}, A = 72 \text{ cm}^2$
4	$a = 13.5 \text{ cm}, b = 8.5 \text{ cm}, c = 19.7 \text{ cm}, h_a = 6.9 \text{ cm}$	$u = 41.7 \text{ cm}, A = 46.7 \text{ cm}^2$
5	$a = 11.7 \text{ cm}, b = 17.3 \text{ cm}, c = 25.5 \text{ cm}, h_a = 14.7 \text{ cm}$	$u = 54.5 \text{ cm}, A = 85.9 \text{ cm}^2$
6	$a = 5.1 \text{ cm}, b = 18.1 \text{ cm}, c = 13.9 \text{ cm}, h_c = 3.3 \text{ cm}$	$u = 37.1 \text{ cm}, A = 22.8 \text{ cm}^2$
7	$a = 15.7 \text{ cm}, b = 14.3 \text{ cm}, c = 28.7 \text{ cm}, h_b = 8.8 \text{ cm}$	$u = 58.7 \text{ cm}, A = 62.6 \text{ cm}^2$
8	$a = 19.8 \text{ cm}, b = 6.8 \text{ cm}, c = 22 \text{ cm}, h_b = 19.5 \text{ cm}$	$u = 48.6 \text{ cm}, A = 66.3 \text{ cm}^2$
9	$a = 15 \text{ cm}, b = 19.3 \text{ cm}, c = 6.3 \text{ cm}, h_b = 4 \text{ cm}$	$u = 40.6 \text{ cm}, A = 38.8 \text{ cm}^2$
10	$a = 19 \text{ cm}, b = 15.1 \text{ cm}, c = 29.7 \text{ cm}, h_c = 8.3 \text{ cm}$	$u = 63.8 \text{ cm}, A = 123.3 \text{ cm}^2$
11	$a = 12.1 \text{ cm}, b = 18.7 \text{ cm}, c = 10.1 \text{ cm}, h_b = 5.9 \text{ cm}$	$u = 40.9 \text{ cm}, A = 55.6 \text{ cm}^2$
12	$a = 7.3 \text{ cm}, b = 15 \text{ cm}, c = 10.9 \text{ cm}, h_a = 10.3 \text{ cm}$	$u = 33.2 \text{ cm}, A = 37.5 \text{ cm}^2$
13	$a = 12.2 \text{ cm}, b = 8.8 \text{ cm}, c = 11.1 \text{ cm}, h_a = 7.7 \text{ cm}$	$u = 32.1 \text{ cm}, A = 47.1 \text{ cm}^2$
14	$a = 14.6 \text{ cm}, b = 11.4 \text{ cm}, c = 14 \text{ cm}, h_c = 10.7 \text{ cm}$	$u = 40 \text{ cm}, A = 74.7 \text{ cm}^2$
15	$a = 17.1 \text{ cm}, b = 6.3 \text{ cm}, c = 12 \text{ cm}, h_a = 3.1 \text{ cm}$	$u = 35.4 \text{ cm}, A = 26.3 \text{ cm}^2$
16	$a = 18.1 \text{ cm}, b = 12 \text{ cm}, c = 26.4 \text{ cm}, h_b = 15.5 \text{ cm}$	$u = 56.5 \text{ cm}, A = 92.8 \text{ cm}^2$
17	$a = 7.6 \text{ cm}, b = 10.5 \text{ cm}, c = 13.4 \text{ cm}, h_a = 10.5 \text{ cm}$	$u = 31.5 \text{ cm}, A = 39.8 \text{ cm}^2$
18	$a = 7.7 \text{ cm}, b = 5.6 \text{ cm}, c = 8.8 \text{ cm}, h_c = 4.8 \text{ cm}$	$u = 22.1 \text{ cm}, A = 21.3 \text{ cm}^2$
19	$a = 10.8 \text{ cm}, b = 12.8 \text{ cm}, c = 11.7 \text{ cm}, h_c = 10.1 \text{ cm}$	$u = 35.3 \text{ cm}, A = 59.1 \text{ cm}^2$
20	$a = 17.8 \text{ cm}, b = 6.6 \text{ cm}, c = 12.5 \text{ cm}, h_b = 8.8 \text{ cm}$	$u = 36.9 \text{ cm}, A = 29.1 \text{ cm}^2$

**Aufgabe 3:** Berechne Umfang und Flächeninhalt des allgemeinen Dreiecks (Seiten a, b, c, Höhen  $h_a$ ,  $h_b$ ,  $h_c$ , u = Umfang, A = Flächeninhalt).

Nr.	Gegeben:
1	a = 6.9 cm, b = 12.4 cm, c = 17.3 cm, $h_b = 5.7$ cm
2	a = 15.3 dm, b = 5.5 dm, c = 15.3 dm, $h_b = 15.1$ dm
3	a = 15.3 mm, b = 18 mm, c = 7.1 mm, $h_a = 7$ mm
4	a = 23.8 cm, b = 18.8 cm, c = 7.5 cm, $h_c = 15.6$ cm
5	a = 6.6 mm, b = 11.5 mm, c = 9.9 mm, $h_a = 9.9$ mm
6	a = 4.8 m, b = 7.7 m, c = 8.5 m, $h_b = 4.8$ m
7	a = 7.4 dm, b = 22.3 dm, c = 22.7 dm, $h_a = 22.2$ dm
8	a = 19.8 dm, b = 12.3 dm, c = 21.6 dm, $h_a = 12.1$ dm
9	a = 11.7 m, b = 9 m, c = 15.9 m, $h_c = 6.5$ m
10	a = 21.3 mm, b = 13.8 mm, c = 14 mm, $h_c = 13.6$ mm
11	a = 22.5 dm, b = 14.5 dm, c = 14.3 dm, $h_b = 13.9$ dm
12	a = 21.4 m, b = 9 m, c = 15.6 m, $h_a = 5.8$ m
13	a = 20.4 mm, b = 13.1 mm, c = 13.8 mm, $h_a = 8.8$ mm
14	a = 23 dm, b = 9 dm, c = 25.7 dm, $h_c = 8$ dm
15	a = 12.7 cm, b = 14.3 cm, c = 23.4 cm, $h_a = 12.4$ cm
16	a = 17.6 m, b = 16.2 m, c = 32.8 m, $h_c = 4.1$ m
17	a = 22.4 dm, b = 10.1 dm, c = 24.9 dm, $h_b = 22.4$ dm
18	a = 20.3 dm, b = 24.2 dm, c = 21 dm, $h_a = 19.9$ dm
19	a = 23.5 dm, b = 15.3 dm, c = 12 dm, $h_c = 13.5$ dm
20	a = 9.1 mm, b = 16.8 mm, c = 17.3 mm, $h_b = 8.9$ mm

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	a = 6.9 cm, b = 12.4 cm, c = 17.3 cm, $h_b = 5.7$ cm	u = 36.6 cm, A = 35.1 cm <sup>2</sup>
2	a = 15.3 dm, b = 5.5 dm, c = 15.3 dm, $h_b = 15.1$ dm	u = 36.1 dm, A = 41.4 dm <sup>2</sup>
3	a = 15.3 mm, b = 18 mm, c = 7.1 mm, $h_a = 7$ mm	u = 40.4 mm, A = 53.4 mm <sup>2</sup>
4	a = 23.8 cm, b = 18.8 cm, c = 7.5 cm, $h_c = 15.6$ cm	u = 50.1 cm, A = 58.6 cm <sup>2</sup>
5	a = 6.6 mm, b = 11.5 mm, c = 9.9 mm, $h_a = 9.9$ mm	u = 28 mm, A = 32.6 mm <sup>2</sup>
6	a = 4.8 m, b = 7.7 m, c = 8.5 m, $h_b = 4.8$ m	u = 21 m, A = 18.3 m <sup>2</sup>
7	a = 7.4 dm, b = 22.3 dm, c = 22.7 dm, $h_a = 22.2$ dm	u = 52.4 dm, A = 82 dm <sup>2</sup>
8	a = 19.8 dm, b = 12.3 dm, c = 21.6 dm, $h_a = 12.1$ dm	u = 53.7 dm, A = 120.2 dm <sup>2</sup>
9	a = 11.7 m, b = 9 m, c = 15.9 m, $h_c = 6.5$ m	u = 36.6 m, A = 51.9 m <sup>2</sup>
10	a = 21.3 mm, b = 13.8 mm, c = 14 mm, $h_c = 13.6$ mm	u = 49.1 mm, A = 95.1 mm <sup>2</sup>
11	a = 22.5 dm, b = 14.5 dm, c = 14.3 dm, $h_b = 13.9$ dm	u = 51.3 dm, A = 101.1 dm <sup>2</sup>
12	a = 21.4 m, b = 9 m, c = 15.6 m, $h_a = 5.8$ m	u = 46 m, A = 61.7 m <sup>2</sup>
13	a = 20.4 mm, b = 13.1 mm, c = 13.8 mm, $h_a = 8.8$ mm	u = 47.3 mm, A = 89.4 mm <sup>2</sup>
14	a = 23 dm, b = 9 dm, c = 25.7 dm, $h_c = 8$ dm	u = 57.7 dm, A = 102.7 dm <sup>2</sup>

15	a = 12.7 cm, b = 14.3 cm, c = 23.4 cm, h <sub>a</sub> = 12.4 cm	u = 50.4 cm, A = 78.6 cm <sup>2</sup>
16	a = 17.6 m, b = 16.2 m, c = 32.8 m, h <sub>c</sub> = 4.1 m	u = 66.6 m, A = 66.9 m <sup>2</sup>
17	a = 22.4 dm, b = 10.1 dm, c = 24.9 dm, h <sub>b</sub> = 22.4 dm	u = 57.4 dm, A = 113 dm <sup>2</sup>
18	a = 20.3 dm, b = 24.2 dm, c = 21 dm, h <sub>a</sub> = 19.9 dm	u = 65.5 dm, A = 202.4 dm <sup>2</sup>
19	a = 23.5 dm, b = 15.3 dm, c = 12 dm, h <sub>c</sub> = 13.5 dm	u = 50.8 dm, A = 80.8 dm <sup>2</sup>
20	a = 9.1 mm, b = 16.8 mm, c = 17.3 mm, h <sub>b</sub> = 8.9 mm	u = 43.2 mm, A = 74.7 mm <sup>2</sup>

**Aufgabe 4:** Berechne Umfang, Flächeninhalt und die fehlenden Höhen des allgemeinen Dreiecks (Seiten a, b, c, Höhen h<sub>a</sub>, h<sub>b</sub>, h<sub>c</sub>, u = Umfang, A = Flächeninhalt).

Nr.	Gegeben:
1	a = 7.1 cm, b = 1.4 cm, c = 7.9 cm, h <sub>a</sub> = 1.2 cm
2	a = 7 cm, b = 2.6 cm, c = 7.4 cm, h <sub>a</sub> = 2.6 cm
3	a = 6.7 cm, b = 2 cm, c = 7.6 cm, h <sub>a</sub> = 1.9 cm
4	a = 8.4 cm, b = 2.7 cm, c = 9.7 cm, h <sub>a</sub> = 2.5 cm
5	a = 7.8 cm, b = 6.6 cm, c = 13.5 cm, h <sub>c</sub> = 2.5 cm
6	a = 9.3 cm, b = 3.9 cm, c = 11.4 cm, h <sub>b</sub> = 8.6 cm
7	a = 9.8 cm, b = 1.6 cm, c = 11.1 cm, h <sub>a</sub> = 1 cm
8	a = 5.1 cm, b = 6 cm, c = 9.1 cm, h <sub>c</sub> = 3.2 cm
9	a = 2.3 cm, b = 1.3 cm, c = 3.1 cm, h <sub>a</sub> = 1.2 cm
10	a = 7.5 cm, b = 2 cm, c = 5.6 cm, h <sub>c</sub> = 0.7 cm
11	a = 6.1 cm, b = 7.1 cm, c = 10.9 cm, h <sub>b</sub> = 5.7 cm
12	a = 4.4 cm, b = 8.1 cm, c = 9.3 cm, h <sub>c</sub> = 3.8 cm
13	a = 4.4 cm, b = 8.5 cm, c = 10.8 cm, h <sub>b</sub> = 4.1 cm
14	a = 6.8 cm, b = 5.3 cm, c = 10.7 cm, h <sub>c</sub> = 2.8 cm
15	a = 8.1 cm, b = 1 cm, c = 8.2 cm, h <sub>a</sub> = 1 cm
16	a = 9.6 cm, b = 6.1 cm, c = 7.1 cm, h <sub>a</sub> = 4.5 cm
17	a = 9.5 cm, b = 7.4 cm, c = 10.4 cm, h <sub>c</sub> = 6.5 cm
18	a = 2.4 cm, b = 3.2 cm, c = 2.2 cm, h <sub>b</sub> = 1.6 cm
19	a = 4 cm, b = 5.9 cm, c = 3.9 cm, h <sub>c</sub> = 4 cm
20	a = 2.1 cm, b = 2.1 cm, c = 1.2 cm, h <sub>a</sub> = 1.1 cm

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	a = 7.1 cm, b = 1.4 cm, c = 7.9 cm, h <sub>a</sub> = 1.2 cm	a = 7.1 cm, b = 1.4 cm, c = 7.9 cm, h <sub>a</sub> = 1.2 cm, h <sub>b</sub> = 6.1 cm, h <sub>c</sub> = 1.1 cm, u = 16.4 cm, A = 4.3 cm <sup>2</sup> , u = 16.4 cm
2	a = 7 cm, b = 2.6 cm, c = 7.4 cm, h <sub>a</sub> = 2.6 cm	a = 7 cm, b = 2.6 cm, c = 7.4 cm, h <sub>a</sub> = 2.6 cm, h <sub>b</sub> = 7 cm, h <sub>c</sub> = 2.5 cm, u = 17 cm, A = 9.1 cm <sup>2</sup>
3	a = 6.7 cm, b = 2 cm, c = 7.6 cm, h <sub>a</sub> = 1.9 cm	a = 6.7 cm, b = 2 cm, c = 7.6 cm, h <sub>a</sub> = 1.9 cm, h <sub>b</sub> = 6.3 cm, h <sub>c</sub> = 1.7 cm, u = 16.3 cm, A = 6.3 cm <sup>2</sup>
4	a = 8.4 cm, b = 2.7 cm, c = 9.7 cm, h <sub>a</sub> = 2.5 cm	a = 8.4 cm, b = 2.7 cm, c = 9.7 cm, h <sub>a</sub> = 2.5 cm, h <sub>b</sub> = 7.8 cm, h <sub>c</sub> = 2.2 cm, u = 20.8 cm, A = 10.6 cm <sup>2</sup>

5	a = 7.8 cm, b = 6.6 cm, c = 13.5 cm, h <sub>c</sub> = 2.5 cm	a = 7.8 cm, b = 6.6 cm, c = 13.5 cm, h <sub>a</sub> = 4.3 cm, h <sub>b</sub> = 5.1 cm, h <sub>c</sub> = 2.5 cm, u = 27.9 cm, A = 16.8 cm <sup>2</sup>
6	a = 9.3 cm, b = 3.9 cm, c = 11.4 cm, h <sub>b</sub> = 8.6 cm	a = 9.3 cm, b = 3.9 cm, c = 11.4 cm, h <sub>a</sub> = 3.6 cm, h <sub>b</sub> = 8.6 cm, h <sub>c</sub> = 2.9 cm, u = 24.6 cm, A = 16.7 cm <sup>2</sup>
7	a = 9.8 cm, b = 1.6 cm, c = 11.1 cm, h <sub>a</sub> = 1 cm	a = 9.8 cm, b = 1.6 cm, c = 11.1 cm, h <sub>a</sub> = 1 cm, h <sub>b</sub> = 6.1 cm, h <sub>c</sub> = 0.9 cm, u = 22.5 cm, A = 4.9 cm <sup>2</sup>
8	a = 5.1 cm, b = 6 cm, c = 9.1 cm, h <sub>c</sub> = 3.2 cm	a = 5.1 cm, b = 6 cm, c = 9.1 cm, h <sub>a</sub> = 5.6 cm, h <sub>b</sub> = 4.8 cm, h <sub>c</sub> = 3.2 cm, u = 20.2 cm, A = 14.4 cm <sup>2</sup>
9	a = 2.3 cm, b = 1.3 cm, c = 3.1 cm, h <sub>a</sub> = 1.2 cm	a = 2.3 cm, b = 1.3 cm, c = 3.1 cm, h <sub>a</sub> = 1.2 cm, h <sub>b</sub> = 2.1 cm, h <sub>c</sub> = 0.9 cm, u = 6.7 cm, A = 1.3 cm <sup>2</sup>
10	a = 7.5 cm, b = 2 cm, c = 5.6 cm, h <sub>c</sub> = 0.7 cm	a = 7.5 cm, b = 2 cm, c = 5.6 cm, h <sub>a</sub> = 0.5 cm, h <sub>b</sub> = 2 cm, h <sub>c</sub> = 0.7 cm, u = 15.1 cm, A = 2 cm <sup>2</sup>
11	a = 6.1 cm, b = 7.1 cm, c = 10.9 cm, h <sub>b</sub> = 5.7 cm	a = 6.1 cm, b = 7.1 cm, c = 10.9 cm, h <sub>a</sub> = 6.6 cm, h <sub>b</sub> = 5.7 cm, h <sub>c</sub> = 3.7 cm, u = 24.1 cm, A = 20.2 cm <sup>2</sup>
12	a = 4.4 cm, b = 8.1 cm, c = 9.3 cm, h <sub>c</sub> = 3.8 cm	a = 4.4 cm, b = 8.1 cm, c = 9.3 cm, h <sub>a</sub> = 8.1 cm, h <sub>b</sub> = 4.4 cm, h <sub>c</sub> = 3.8 cm, u = 21.8 cm, A = 17.8 cm <sup>2</sup>
13	a = 4.4 cm, b = 8.5 cm, c = 10.8 cm, h <sub>b</sub> = 4.1 cm	a = 4.4 cm, b = 8.5 cm, c = 10.8 cm, h <sub>a</sub> = 8 cm, h <sub>b</sub> = 4.1 cm, h <sub>c</sub> = 3.3 cm, u = 23.7 cm, A = 17.6 cm <sup>2</sup>
14	a = 6.8 cm, b = 5.3 cm, c = 10.7 cm, h <sub>c</sub> = 2.8 cm	a = 6.8 cm, b = 5.3 cm, c = 10.7 cm, h <sub>a</sub> = 4.4 cm, h <sub>b</sub> = 5.6 cm, h <sub>c</sub> = 2.8 cm, u = 22.8 cm, A = 15 cm <sup>2</sup>
15	a = 8.1 cm, b = 1 cm, c = 8.2 cm, h <sub>a</sub> = 1 cm	a = 8.1 cm, b = 1 cm, c = 8.2 cm, h <sub>a</sub> = 1 cm, h <sub>b</sub> = 8.1 cm, h <sub>c</sub> = 1 cm, u = 17.3 cm, A = 4 cm <sup>2</sup>
16	a = 9.6 cm, b = 6.1 cm, c = 7.1 cm, h <sub>a</sub> = 4.5 cm	a = 9.6 cm, b = 6.1 cm, c = 7.1 cm, h <sub>a</sub> = 4.5 cm, h <sub>b</sub> = 7.1 cm, h <sub>c</sub> = 6.1 cm, u = 22.8 cm, A = 21.6 cm <sup>2</sup>
17	a = 9.5 cm, b = 7.4 cm, c = 10.4 cm, h <sub>c</sub> = 6.5 cm	a = 9.5 cm, b = 7.4 cm, c = 10.4 cm, h <sub>a</sub> = 7.1 cm, h <sub>b</sub> = 9.2 cm, h <sub>c</sub> = 6.5 cm, u = 27.3 cm, A = 33.9 cm <sup>2</sup>
18	a = 2.4 cm, b = 3.2 cm, c = 2.2 cm, h <sub>b</sub> = 1.6 cm	a = 2.4 cm, b = 3.2 cm, c = 2.2 cm, h <sub>a</sub> = 2.2 cm, h <sub>b</sub> = 1.6 cm, h <sub>c</sub> = 2.4 cm, u = 7.8 cm, A = 2.6 cm <sup>2</sup>
19	a = 4 cm, b = 5.9 cm, c = 3.9 cm, h <sub>c</sub> = 4 cm	a = 4 cm, b = 5.9 cm, c = 3.9 cm, h <sub>a</sub> = 3.9 cm, h <sub>b</sub> = 2.6 cm, h <sub>c</sub> = 4 cm, u = 13.8 cm, A = 7.7 cm <sup>2</sup>
20	a = 2.1 cm, b = 2.1 cm, c = 1.2 cm, h <sub>a</sub> = 1.1 cm	a = 2.1 cm, b = 2.1 cm, c = 1.2 cm, h <sub>a</sub> = 1.1 cm, h <sub>b</sub> = 1.1 cm, h <sub>c</sub> = 2 cm, u = 5.4 cm, A = 1.2 cm <sup>2</sup>

**Aufgabe 5:** Berechne Umfang, Flächeninhalt und die fehlenden Höhen des allgemeinen Dreiecks (Seiten a, b, c, Höhen h<sub>a</sub>, h<sub>b</sub>, h<sub>c</sub>, u = Umfang, A = Flächeninhalt).

Nr.	Gegeben:
1	a = 9.9 cm, b = 14 cm, c = 13.4 cm, h <sub>b</sub> = 9 cm
2	a = 13.7 mm, b = 9.5 mm, c = 12.8 mm, h <sub>b</sub> = 12.3 mm
3	a = 19.8 dm, b = 11.8 dm, c = 26.1 dm, h <sub>a</sub> = 11.2 dm
4	a = 19.1 mm, b = 15.8 mm, c = 20 mm, h <sub>c</sub> = 14.1 mm
5	a = 5 mm, b = 13.2 mm, c = 17.6 mm, h <sub>b</sub> = 2.7 mm
6	a = 10.1 dm, b = 6 dm, c = 9.2 dm, h <sub>b</sub> = 9.1 dm
7	a = 16.8 mm, b = 17 mm, c = 24.7 mm, h <sub>a</sub> = 17 mm
8	a = 12.2 mm, b = 12.9 mm, c = 16.2 mm, h <sub>b</sub> = 12 mm
9	a = 8.9 mm, b = 8.6 mm, c = 6.4 mm, h <sub>b</sub> = 6.1 mm
10	a = 10.3 m, b = 9.5 m, c = 4 m, h <sub>b</sub> = 4 m
11	a = 13.5 mm, b = 13.1 mm, c = 8.7 mm, h <sub>b</sub> = 8.3 mm
12	a = 19.7 m, b = 15.6 m, c = 22.5 m, h <sub>a</sub> = 15.3 m
13	a = 19 cm, b = 13.2 cm, c = 7.1 cm, h <sub>b</sub> = 4.9 cm

14	$a = 15.9 \text{ mm}, b = 11.2 \text{ mm}, c = 17.1 \text{ mm}, h_a = 10.9 \text{ mm}$
15	$a = 17.2 \text{ cm}, b = 9.1 \text{ cm}, c = 20.1 \text{ cm}, h_a = 9.1 \text{ cm}$
16	$a = 19.6 \text{ dm}, b = 15.8 \text{ dm}, c = 19.1 \text{ dm}, h_b = 17.7 \text{ dm}$
17	$a = 18 \text{ m}, b = 16.4 \text{ m}, c = 27.7 \text{ m}, h_a = 15.7 \text{ m}$
18	$a = 6.9 \text{ dm}, b = 12.5 \text{ dm}, c = 6.5 \text{ dm}, h_a = 4.4 \text{ dm}$
19	$a = 4.9 \text{ mm}, b = 18.9 \text{ mm}, c = 20.7 \text{ mm}, h_a = 18.3 \text{ mm}$
20	$a = 10.4 \text{ mm}, b = 12.2 \text{ mm}, c = 12.5 \text{ mm}, h_b = 9.5 \text{ mm}$

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	$a = 9.9 \text{ cm}, b = 14 \text{ cm}, c = 13.4 \text{ cm}, h_b = 9 \text{ cm}$	$a = 9.9 \text{ cm}, b = 14 \text{ cm}, c = 13.4 \text{ cm}, h_a = 12.8 \text{ cm}, h_b = 9 \text{ cm}, h_c = 9.4 \text{ cm}, u = 37.3 \text{ cm}, A = 63.1 \text{ cm}^2$
2	$a = 13.7 \text{ mm}, b = 9.5 \text{ mm}, c = 12.8 \text{ mm}, h_b = 12.3 \text{ mm}$	$a = 13.7 \text{ mm}, b = 9.5 \text{ mm}, c = 12.8 \text{ mm}, h_a = 8.5 \text{ mm}, h_b = 12.3 \text{ mm}, h_c = 9.1 \text{ mm}, u = 36 \text{ mm}, A = 58.5 \text{ mm}^2$
3	$a = 19.8 \text{ dm}, b = 11.8 \text{ dm}, c = 26.1 \text{ dm}, h_a = 11.2 \text{ dm}$	$a = 19.8 \text{ dm}, b = 11.8 \text{ dm}, c = 26.1 \text{ dm}, h_a = 11.2 \text{ dm}, h_b = 18.8 \text{ dm}, h_c = 8.5 \text{ dm}, u = 57.7 \text{ dm}, A = 110.6 \text{ dm}^2$
4	$a = 19.1 \text{ mm}, b = 15.8 \text{ mm}, c = 20 \text{ mm}, h_c = 14.1 \text{ mm}$	$a = 19.1 \text{ mm}, b = 15.8 \text{ mm}, c = 20 \text{ mm}, h_a = 14.8 \text{ mm}, h_b = 17.9 \text{ mm}, h_c = 14.1 \text{ mm}, u = 54.9 \text{ mm}, A = 141 \text{ mm}^2$
5	$a = 5 \text{ mm}, b = 13.2 \text{ mm}, c = 17.6 \text{ mm}, h_b = 2.7 \text{ mm}$	$a = 5 \text{ mm}, b = 13.2 \text{ mm}, c = 17.6 \text{ mm}, h_a = 7.2 \text{ mm}, h_b = 2.7 \text{ mm}, h_c = 2.1 \text{ mm}, u = 35.8 \text{ mm}, A = 18 \text{ mm}^2$
6	$a = 10.1 \text{ dm}, b = 6 \text{ dm}, c = 9.2 \text{ dm}, h_b = 9.1 \text{ dm}$	$a = 10.1 \text{ dm}, b = 6 \text{ dm}, c = 9.2 \text{ dm}, h_a = 5.4 \text{ dm}, h_b = 9.1 \text{ dm}, h_c = 5.9 \text{ dm}, u = 25.3 \text{ dm}, A = 27.2 \text{ dm}^2$
7	$a = 16.8 \text{ mm}, b = 17 \text{ mm}, c = 24.7 \text{ mm}, h_a = 17 \text{ mm}$	$a = 16.8 \text{ mm}, b = 17 \text{ mm}, c = 24.7 \text{ mm}, h_a = 17 \text{ mm}, h_b = 16.8 \text{ mm}, h_c = 11.5 \text{ mm}, u = 58.5 \text{ mm}, A = 142.5 \text{ mm}^2$
8	$a = 12.2 \text{ mm}, b = 12.9 \text{ mm}, c = 16.2 \text{ mm}, h_b = 12 \text{ mm}$	$a = 12.2 \text{ mm}, b = 12.9 \text{ mm}, c = 16.2 \text{ mm}, h_a = 12.7 \text{ mm}, h_b = 12 \text{ mm}, h_c = 9.6 \text{ mm}, u = 41.3 \text{ mm}, A = 77.6 \text{ mm}^2$
9	$a = 8.9 \text{ mm}, b = 8.6 \text{ mm}, c = 6.4 \text{ mm}, h_b = 6.1 \text{ mm}$	$a = 8.9 \text{ mm}, b = 8.6 \text{ mm}, c = 6.4 \text{ mm}, h_a = 5.8 \text{ mm}, h_b = 6.1 \text{ mm}, h_c = 8.1 \text{ mm}, u = 23.9 \text{ mm}, A = 26 \text{ mm}^2$
10	$a = 10.3 \text{ m}, b = 9.5 \text{ m}, c = 4 \text{ m}, h_b = 4 \text{ m}$	$a = 10.3 \text{ m}, b = 9.5 \text{ m}, c = 4 \text{ m}, h_a = 3.7 \text{ m}, h_b = 4 \text{ m}, h_c = 9.5 \text{ m}, u = 23.8 \text{ m}, A = 19 \text{ m}^2$
11	$a = 13.5 \text{ mm}, b = 13.1 \text{ mm}, c = 8.7 \text{ mm}, h_b = 8.3 \text{ mm}$	$a = 13.5 \text{ mm}, b = 13.1 \text{ mm}, c = 8.7 \text{ mm}, h_a = 8.1 \text{ mm}, h_b = 8.3 \text{ mm}, h_c = 12.6 \text{ mm}, u = 35.3 \text{ mm}, A = 54.6 \text{ mm}^2$
12	$a = 19.7 \text{ m}, b = 15.6 \text{ m}, c = 22.5 \text{ m}, h_a = 15.3 \text{ m}$	$a = 19.7 \text{ m}, b = 15.6 \text{ m}, c = 22.5 \text{ m}, h_a = 15.3 \text{ m}, h_b = 19.3 \text{ m}, h_c = 13.4 \text{ m}, u = 57.8 \text{ m}, A = 150.4 \text{ m}^2$
13	$a = 19 \text{ cm}, b = 13.2 \text{ cm}, c = 7.1 \text{ cm}, h_b = 4.9 \text{ cm}$	$a = 19 \text{ cm}, b = 13.2 \text{ cm}, c = 7.1 \text{ cm}, h_a = 3.4 \text{ cm}, h_b = 4.9 \text{ cm}, h_c = 9.1 \text{ cm}, u = 39.3 \text{ cm}, A = 32.2 \text{ cm}^2$
14	$a = 15.9 \text{ mm}, b = 11.2 \text{ mm}, c = 17.1 \text{ mm}, h_a = 10.9 \text{ mm}$	$a = 15.9 \text{ mm}, b = 11.2 \text{ mm}, c = 17.1 \text{ mm}, h_a = 10.9 \text{ mm}, h_b = 15.4 \text{ mm}, h_c = 10.1 \text{ mm}, u = 44.2 \text{ mm}, A = 86.4 \text{ mm}^2$
15	$a = 17.2 \text{ cm}, b = 9.1 \text{ cm}, c = 20.1 \text{ cm}, h_a = 9.1 \text{ cm}$	$a = 17.2 \text{ cm}, b = 9.1 \text{ cm}, c = 20.1 \text{ cm}, h_a = 9.1 \text{ cm}, h_b = 17.1 \text{ cm}, h_c = 7.8 \text{ cm}, u = 46.4 \text{ cm}, A = 78 \text{ cm}^2$
16	$a = 19.6 \text{ dm}, b = 15.8 \text{ dm}, c = 19.1 \text{ dm}, h_b = 17.7 \text{ dm}$	$a = 19.6 \text{ dm}, b = 15.8 \text{ dm}, c = 19.1 \text{ dm}, h_a = 14.2 \text{ dm}, h_b = 17.7 \text{ dm}, h_c = 14.6 \text{ dm}, u = 54.5 \text{ dm}, A = 139.5 \text{ dm}^2$
17	$a = 18 \text{ m}, b = 16.4 \text{ m}, c = 27.7 \text{ m}, h_a = 15.7 \text{ m}$	$a = 18 \text{ m}, b = 16.4 \text{ m}, c = 27.7 \text{ m}, h_a = 15.7 \text{ m}, h_b = 17.2 \text{ m}, h_c = 10.2 \text{ m}, u = 62.1 \text{ m}, A = 141 \text{ m}^2$
18	$a = 6.9 \text{ dm}, b = 12.5 \text{ dm}, c = 6.5 \text{ dm}, h_a = 4.4 \text{ dm}$	$a = 6.9 \text{ dm}, b = 12.5 \text{ dm}, c = 6.5 \text{ dm}, h_a = 4.4 \text{ dm}, h_b = 2.4 \text{ dm}, h_c = 4.6 \text{ dm}, u = 25.9 \text{ dm}, A = 15.1 \text{ dm}^2$
19	$a = 4.9 \text{ mm}, b = 18.9 \text{ mm}, c = 20.7 \text{ mm}, h_a = 18.3 \text{ mm}$	$a = 4.9 \text{ mm}, b = 18.9 \text{ mm}, c = 20.7 \text{ mm}, h_a = 18.3 \text{ mm}, h_b = 4.7 \text{ mm}, h_c = 4.3 \text{ mm}, u = 44.5 \text{ mm}, A = 44.8 \text{ mm}^2$
20	$a = 10.4 \text{ mm}, b = 12.2 \text{ mm}, c = 12.5 \text{ mm}, h_b = 9.5 \text{ mm}$	$a = 10.4 \text{ mm}, b = 12.2 \text{ mm}, c = 12.5 \text{ mm}, h_a = 11.2 \text{ mm}, h_b = 9.5 \text{ mm}, h_c = 9.3 \text{ mm}, u = 35.1 \text{ mm}, A = 58.2 \text{ mm}^2$

**Aufgabe 6:** Berechne die fehlende Seite, die fehlenden Höhen und den Umfang des allgemeinen Dreiecks (Seiten  $a$ ,  $b$ ,  $c$ , Höhen  $h_a$ ,  $h_b$ ,  $h_c$ ,  $u$  = Umfang,  $A$  = Flächeninhalt).

Nr.	Gegeben:
1	$b = 5.8 \text{ cm}$ , $c = 6.1 \text{ cm}$ , $h_a = 4.7 \text{ cm}$ , $A = 17 \text{ cm}^2$
2	$b = 6 \text{ cm}$ , $c = 8.7 \text{ cm}$ , $h_a = 3.1 \text{ cm}$ , $A = 4.7 \text{ cm}^2$
3	$a = 2.1 \text{ cm}$ , $c = 7.6 \text{ cm}$ , $h_b = 1.7 \text{ cm}$ , $A = 7.2 \text{ cm}^2$
4	$a = 8 \text{ cm}$ , $c = 6.3 \text{ cm}$ , $h_b = 5.1 \text{ cm}$ , $A = 25.2 \text{ cm}^2$
5	$a = 4.9 \text{ cm}$ , $c = 8.6 \text{ cm}$ , $h_b = 4.5 \text{ cm}$ , $A = 20.8 \text{ cm}^2$
6	$b = 3.8 \text{ cm}$ , $c = 5.4 \text{ cm}$ , $h_a = 1.3 \text{ cm}$ , $A = 5.8 \text{ cm}^2$
7	$a = 4.9 \text{ cm}$ , $b = 4.4 \text{ cm}$ , $h_c = 3.6 \text{ cm}$ , $A = 10.6 \text{ cm}^2$
8	$a = 1 \text{ cm}$ , $c = 2.9 \text{ cm}$ , $h_b = 1 \text{ cm}$ , $A = 1.4 \text{ cm}^2$
9	$b = 6.3 \text{ cm}$ , $c = 6 \text{ cm}$ , $h_a = 6 \text{ cm}$ , $A = 4.8 \text{ cm}^2$
10	$a = 8.7 \text{ cm}$ , $b = 9.2 \text{ cm}$ , $h_c = 6.6 \text{ cm}$ , $A = 39.9 \text{ cm}^2$
11	$a = 6.6 \text{ cm}$ , $c = 5.5 \text{ cm}$ , $h_b = 4.7 \text{ cm}$ , $A = 17.6 \text{ cm}^2$
12	$a = 9.2 \text{ cm}$ , $b = 6.7 \text{ cm}$ , $h_c = 5.6 \text{ cm}$ , $A = 30.7 \text{ cm}^2$
13	$b = 7.6 \text{ cm}$ , $c = 3.2 \text{ cm}$ , $h_a = 3.1 \text{ cm}$ , $A = 9.7 \text{ cm}^2$
14	$a = 7.1 \text{ cm}$ , $b = 4.6 \text{ cm}$ , $h_c = 4.1 \text{ cm}$ , $A = 16.2 \text{ cm}^2$
15	$a = 2.5 \text{ cm}$ , $c = 4.9 \text{ cm}$ , $h_b = 2.5 \text{ cm}$ , $A = 5.2 \text{ cm}^2$
16	$a = 5.8 \text{ cm}$ , $c = 7.9 \text{ cm}$ , $h_b = 5.1 \text{ cm}$ , $A = 22.3 \text{ cm}^2$
17	$a = 2.5 \text{ cm}$ , $b = 5.3 \text{ cm}$ , $h_c = 2.5 \text{ cm}$ , $A = 6 \text{ cm}^2$
18	$b = 9.6 \text{ cm}$ , $c = 8.9 \text{ cm}$ , $h_a = 7.9 \text{ cm}$ , $A = 37.6 \text{ cm}^2$
19	$a = 7.5 \text{ cm}$ , $c = 8.7 \text{ cm}$ , $h_b = 4.8 \text{ cm}$ , $A = 3.6 \text{ cm}^2$
20	$a = 4.4 \text{ cm}$ , $c = 5 \text{ cm}$ , $h_b = 4.4 \text{ cm}$ , $A = 6.3 \text{ cm}^2$

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	$b = 5.8 \text{ cm}$ , $c = 6.1 \text{ cm}$ , $h_a = 4.7 \text{ cm}$ , $A = 17 \text{ cm}^2$	$a = 7.2 \text{ cm}$ , $b = 5.8 \text{ cm}$ , $c = 6.1 \text{ cm}$ , $h_a = 4.7 \text{ cm}$ , $h_b = 5.9 \text{ cm}$ , $h_c = 5.6 \text{ cm}$ , $u = 19.1 \text{ cm}$ , $A = 17 \text{ cm}^2$
2	$b = 6 \text{ cm}$ , $c = 8.7 \text{ cm}$ , $h_a = 3.1 \text{ cm}$ , $A = 4.7 \text{ cm}^2$	$a = 3 \text{ cm}$ , $b = 6 \text{ cm}$ , $c = 8.7 \text{ cm}$ , $h_a = 3.1 \text{ cm}$ , $h_b = 1.6 \text{ cm}$ , $h_c = 1.1 \text{ cm}$ , $u = 17.7 \text{ cm}$ , $A = 4.7 \text{ cm}^2$
3	$a = 2.1 \text{ cm}$ , $c = 7.6 \text{ cm}$ , $h_b = 1.7 \text{ cm}$ , $A = 7.2 \text{ cm}^2$	$a = 2.1 \text{ cm}$ , $b = 8.7 \text{ cm}$ , $c = 7.6 \text{ cm}$ , $h_a = 6.9 \text{ cm}$ , $h_b = 1.7 \text{ cm}$ , $h_c = 1.9 \text{ cm}$ , $u = 18.4 \text{ cm}$ , $A = 7.2 \text{ cm}^2$
4	$a = 8 \text{ cm}$ , $c = 6.3 \text{ cm}$ , $h_b = 5.1 \text{ cm}$ , $A = 25.2 \text{ cm}^2$	$a = 8 \text{ cm}$ , $b = 9.9 \text{ cm}$ , $c = 6.3 \text{ cm}$ , $h_a = 6.3 \text{ cm}$ , $h_b = 5.1 \text{ cm}$ , $h_c = 8 \text{ cm}$ , $u = 24.2 \text{ cm}$ , $A = 25.2 \text{ cm}^2$
5	$a = 4.9 \text{ cm}$ , $c = 8.6 \text{ cm}$ , $h_b = 4.5 \text{ cm}$ , $A = 20.8 \text{ cm}^2$	$a = 4.9 \text{ cm}$ , $b = 9.2 \text{ cm}$ , $c = 8.6 \text{ cm}$ , $h_a = 8.5 \text{ cm}$ , $h_b = 4.5 \text{ cm}$ , $h_c = 4.8 \text{ cm}$ , $u = 22.7 \text{ cm}$ , $A = 20.8 \text{ cm}^2$
6	$b = 3.8 \text{ cm}$ , $c = 5.4 \text{ cm}$ , $h_a = 1.3 \text{ cm}$ , $A = 5.8 \text{ cm}^2$	$a = 8.8 \text{ cm}$ , $b = 3.8 \text{ cm}$ , $c = 5.4 \text{ cm}$ , $h_a = 1.3 \text{ cm}$ , $h_b = 3.1 \text{ cm}$ , $h_c = 2.1 \text{ cm}$ , $u = 18 \text{ cm}$ , $A = 5.8 \text{ cm}^2$
7	$a = 4.9 \text{ cm}$ , $b = 4.4 \text{ cm}$ , $h_c = 3.6 \text{ cm}$ , $A = 10.6 \text{ cm}^2$	$a = 4.9 \text{ cm}$ , $b = 4.4 \text{ cm}$ , $c = 5.9 \text{ cm}$ , $h_a = 4.3 \text{ cm}$ , $h_b = 4.8 \text{ cm}$ , $h_c = 3.6 \text{ cm}$ , $u = 15.2 \text{ cm}$ , $A = 10.6 \text{ cm}^2$
8	$a = 1 \text{ cm}$ , $c = 2.9 \text{ cm}$ , $h_b = 1 \text{ cm}$ , $A = 1.4 \text{ cm}^2$	$a = 1 \text{ cm}$ , $b = 2.8 \text{ cm}$ , $c = 2.9 \text{ cm}$ , $h_a = 2.8 \text{ cm}$ , $h_b = 1 \text{ cm}$ , $h_c = 1 \text{ cm}$ , $u = 6.7 \text{ cm}$ , $A = 1.4 \text{ cm}^2$
9	$b = 6.3 \text{ cm}$ , $c = 6 \text{ cm}$ , $h_a = 6 \text{ cm}$ , $A = 4.8 \text{ cm}^2$	$a = 1.6 \text{ cm}$ , $b = 6.3 \text{ cm}$ , $c = 6 \text{ cm}$ , $h_a = 6 \text{ cm}$ , $h_b = 1.5 \text{ cm}$ , $h_c = 1.6 \text{ cm}$ , $u = 13.9 \text{ cm}$ , $A = 4.8 \text{ cm}^2$



10	a = 8.7 cm, b = 9.2 cm, h <sub>c</sub> = 6.6 cm, A = 39.9 cm <sup>2</sup>	a = 8.7 cm, b = 9.2 cm, c = 12.1 cm, h <sub>a</sub> = 9.2 cm, h <sub>b</sub> = 8.7 cm, h <sub>c</sub> = 6.6 cm, u = 30 cm, A = 39.9 cm <sup>2</sup>
11	a = 6.6 cm, c = 5.5 cm, h <sub>b</sub> = 4.7 cm, A = 17.6 cm <sup>2</sup>	a = 6.6 cm, b = 7.5 cm, c = 5.5 cm, h <sub>a</sub> = 5.3 cm, h <sub>b</sub> = 4.7 cm, h <sub>c</sub> = 6.4 cm, u = 19.6 cm, A = 17.6 cm <sup>2</sup>
12	a = 9.2 cm, b = 6.7 cm, h <sub>c</sub> = 5.6 cm, A = 30.7 cm <sup>2</sup>	a = 9.2 cm, b = 6.7 cm, c = 10.9 cm, h <sub>a</sub> = 6.7 cm, h <sub>b</sub> = 9.2 cm, h <sub>c</sub> = 5.6 cm, u = 26.8 cm, A = 30.7 cm <sup>2</sup>
13	b = 7.6 cm, c = 3.2 cm, h <sub>a</sub> = 3.1 cm, A = 9.7 cm <sup>2</sup>	a = 6.2 cm, b = 7.6 cm, c = 3.2 cm, h <sub>a</sub> = 3.1 cm, h <sub>b</sub> = 2.5 cm, h <sub>c</sub> = 6 cm, u = 17 cm, A = 9.7 cm <sup>2</sup>
14	a = 7.1 cm, b = 4.6 cm, h <sub>c</sub> = 4.1 cm, A = 16.2 cm <sup>2</sup>	a = 7.1 cm, b = 4.6 cm, c = 8 cm, h <sub>a</sub> = 4.6 cm, h <sub>b</sub> = 7.1 cm, h <sub>c</sub> = 4.1 cm, u = 19.7 cm, A = 16.2 cm <sup>2</sup>
15	a = 2.5 cm, c = 4.9 cm, h <sub>b</sub> = 2.5 cm, A = 5.2 cm <sup>2</sup>	a = 2.5 cm, b = 4.2 cm, c = 4.9 cm, h <sub>a</sub> = 4.2 cm, h <sub>b</sub> = 2.5 cm, h <sub>c</sub> = 2.1 cm, u = 11.6 cm, A = 5.2 cm <sup>2</sup>
16	a = 5.8 cm, c = 7.9 cm, h <sub>b</sub> = 5.1 cm, A = 22.3 cm <sup>2</sup>	a = 5.8 cm, b = 8.7 cm, c = 7.9 cm, h <sub>a</sub> = 7.7 cm, h <sub>b</sub> = 5.1 cm, h <sub>c</sub> = 5.7 cm, u = 22.4 cm, A = 22.3 cm <sup>2</sup>
17	a = 2.5 cm, b = 5.3 cm, h <sub>c</sub> = 2.5 cm, A = 6 cm <sup>2</sup>	a = 2.5 cm, b = 5.3 cm, c = 4.8 cm, h <sub>a</sub> = 4.8 cm, h <sub>b</sub> = 2.3 cm, h <sub>c</sub> = 2.5 cm, u = 12.6 cm, A = 6 cm <sup>2</sup>
18	b = 9.6 cm, c = 8.9 cm, h <sub>a</sub> = 7.9 cm, A = 37.6 cm <sup>2</sup>	a = 9.5 cm, b = 9.6 cm, c = 8.9 cm, h <sub>a</sub> = 7.9 cm, h <sub>b</sub> = 7.8 cm, h <sub>c</sub> = 8.4 cm, u = 28 cm, A = 37.6 cm <sup>2</sup>
19	a = 7.5 cm, c = 8.7 cm, h <sub>b</sub> = 4.8 cm, A = 3.6 cm <sup>2</sup>	a = 7.5 cm, b = 1.5 cm, c = 8.7 cm, h <sub>a</sub> = 1 cm, h <sub>b</sub> = 4.8 cm, h <sub>c</sub> = 0.8 cm, u = 17.7 cm, A = 3.6 cm <sup>2</sup>
20	a = 4.4 cm, c = 5 cm, h <sub>b</sub> = 4.4 cm, A = 6.3 cm <sup>2</sup>	a = 4.4 cm, b = 2.9 cm, c = 5 cm, h <sub>a</sub> = 2.9 cm, h <sub>b</sub> = 4.4 cm, h <sub>c</sub> = 2.5 cm, u = 12.3 cm, A = 6.3 cm <sup>2</sup>

**Aufgabe 7:** Berechne die fehlende Seite, die fehlenden Höhen und den Umfang des allgemeinen Dreiecks (Seiten a, b, c, Höhen h<sub>a</sub>, h<sub>b</sub>, h<sub>c</sub>, u = Umfang, A = Flächeninhalt).

Nr.	Gegeben:
1	b = 20 cm, c = 17.4 cm, h <sub>a</sub> = 15.6 cm, A = 157.2 cm <sup>2</sup>
2	a = 10.4 cm, c = 23.9 cm, h <sub>b</sub> = 10 cm, A = 122.9 cm <sup>2</sup>
3	a = 18.3 cm, c = 15.3 cm, h <sub>b</sub> = 13.9 cm, A = 126.8 cm <sup>2</sup>
4	b = 11.4 cm, c = 11.3 cm, h <sub>a</sub> = 10.8 cm, A = 36.3 cm <sup>2</sup>
5	a = 10.8 cm, c = 15.6 cm, h <sub>b</sub> = 6.6 cm, A = 18.6 cm <sup>2</sup>
6	b = 23.2 cm, c = 29.6 cm, h <sub>a</sub> = 23.1 cm, A = 243.3 cm <sup>2</sup>
7	a = 11.8 cm, b = 19.1 cm, h <sub>c</sub> = 11.8 cm, A = 91.4 cm <sup>2</sup>
8	a = 16.7 cm, b = 14 cm, h <sub>c</sub> = 13.9 cm, A = 73.2 cm <sup>2</sup>
9	a = 16.5 cm, c = 13.9 cm, h <sub>b</sub> = 11.2 cm, A = 114 cm <sup>2</sup>
10	a = 23.8 cm, b = 17.6 cm, h <sub>c</sub> = 8.3 cm, A = 157.4 cm <sup>2</sup>
11	b = 16.1 cm, c = 17.3 cm, h <sub>a</sub> = 13.9 cm, A = 128 cm <sup>2</sup>
12	a = 10.6 cm, c = 22.7 cm, h <sub>b</sub> = 10.6 cm, A = 101.4 cm <sup>2</sup>
13	b = 11.4 cm, c = 13.4 cm, h <sub>a</sub> = 6.4 cm, A = 67.9 cm <sup>2</sup>
14	a = 14.7 cm, c = 12.2 cm, h <sub>b</sub> = 10.6 cm, A = 86.2 cm <sup>2</sup>
15	a = 11.2 cm, c = 15 cm, h <sub>b</sub> = 11 cm, A = 69 cm <sup>2</sup>
16	b = 8.7 cm, c = 11.4 cm, h <sub>a</sub> = 5.7 cm, A = 47 cm <sup>2</sup>
17	b = 10.4 cm, c = 10.2 cm, h <sub>a</sub> = 7.3 cm, A = 53 cm <sup>2</sup>
18	b = 13.7 cm, c = 18.4 cm, h <sub>a</sub> = 9.2 cm, A = 26.8 cm <sup>2</sup>
19	a = 19.6 cm, c = 29.9 cm, h <sub>b</sub> = 19.3 cm, A = 184.8 cm <sup>2</sup>
20	a = 13.9 cm, b = 7.3 cm, h <sub>c</sub> = 6.3 cm, A = 50.6 cm <sup>2</sup>

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	$b = 20 \text{ cm}, c = 17.4 \text{ cm}, h_a = 15.6 \text{ cm}, A = 157.2 \text{ cm}^2$	$a = 20.1 \text{ cm}, b = 20 \text{ cm}, c = 17.4 \text{ cm}, h_a = 15.6 \text{ cm}, h_b = 15.7 \text{ cm}, h_c = 18.1 \text{ cm}, u = 57.5 \text{ cm}, A = 157.2 \text{ cm}^2$
2	$a = 10.4 \text{ cm}, c = 23.9 \text{ cm}, h_b = 10 \text{ cm}, A = 122.9 \text{ cm}^2$	$a = 10.4 \text{ cm}, b = 24.6 \text{ cm}, c = 23.9 \text{ cm}, h_a = 23.6 \text{ cm}, h_b = 10 \text{ cm}, h_c = 10.3 \text{ cm}, u = 58.9 \text{ cm}, A = 122.9 \text{ cm}^2$
3	$a = 18.3 \text{ cm}, c = 15.3 \text{ cm}, h_b = 13.9 \text{ cm}, A = 126.8 \text{ cm}^2$	$a = 18.3 \text{ cm}, b = 18.2 \text{ cm}, c = 15.3 \text{ cm}, h_a = 13.9 \text{ cm}, h_b = 13.9 \text{ cm}, h_c = 16.6 \text{ cm}, u = 51.8 \text{ cm}, A = 126.8 \text{ cm}^2$
4	$b = 11.4 \text{ cm}, c = 11.3 \text{ cm}, h_a = 10.8 \text{ cm}, A = 36.3 \text{ cm}^2$	$a = 6.7 \text{ cm}, b = 11.4 \text{ cm}, c = 11.3 \text{ cm}, h_a = 10.8 \text{ cm}, h_b = 6.4 \text{ cm}, h_c = 6.4 \text{ cm}, u = 29.4 \text{ cm}, A = 36.3 \text{ cm}^2$
5	$a = 10.8 \text{ cm}, c = 15.6 \text{ cm}, h_b = 6.6 \text{ cm}, A = 18.6 \text{ cm}^2$	$a = 10.8 \text{ cm}, b = 5.6 \text{ cm}, c = 15.6 \text{ cm}, h_a = 3.4 \text{ cm}, h_b = 6.6 \text{ cm}, h_c = 2.4 \text{ cm}, u = 32 \text{ cm}, A = 18.6 \text{ cm}^2$
6	$b = 23.2 \text{ cm}, c = 29.6 \text{ cm}, h_a = 23.1 \text{ cm}, A = 243.3 \text{ cm}^2$	$a = 21.1 \text{ cm}, b = 23.2 \text{ cm}, c = 29.6 \text{ cm}, h_a = 23.1 \text{ cm}, h_b = 21 \text{ cm}, h_c = 16.4 \text{ cm}, u = 73.9 \text{ cm}, A = 243.3 \text{ cm}^2$
7	$a = 11.8 \text{ cm}, b = 19.1 \text{ cm}, h_c = 11.8 \text{ cm}, A = 91.4 \text{ cm}^2$	$a = 11.8 \text{ cm}, b = 19.1 \text{ cm}, c = 15.5 \text{ cm}, h_a = 15.5 \text{ cm}, h_b = 9.6 \text{ cm}, h_c = 11.8 \text{ cm}, u = 46.4 \text{ cm}, A = 91.4 \text{ cm}^2$
8	$a = 16.7 \text{ cm}, b = 14 \text{ cm}, h_c = 13.9 \text{ cm}, A = 73.2 \text{ cm}^2$	$a = 16.7 \text{ cm}, b = 14 \text{ cm}, c = 10.5 \text{ cm}, h_a = 8.8 \text{ cm}, h_b = 10.5 \text{ cm}, h_c = 13.9 \text{ cm}, u = 41.2 \text{ cm}, A = 73.2 \text{ cm}^2$
9	$a = 16.5 \text{ cm}, c = 13.9 \text{ cm}, h_b = 11.2 \text{ cm}, A = 114 \text{ cm}^2$	$a = 16.5 \text{ cm}, b = 20.4 \text{ cm}, c = 13.9 \text{ cm}, h_a = 13.8 \text{ cm}, h_b = 11.2 \text{ cm}, h_c = 16.4 \text{ cm}, u = 50.8 \text{ cm}, A = 114 \text{ cm}^2$
10	$a = 23.8 \text{ cm}, b = 17.6 \text{ cm}, h_c = 8.3 \text{ cm}, A = 157.4 \text{ cm}^2$	$a = 23.8 \text{ cm}, b = 17.6 \text{ cm}, c = 37.8 \text{ cm}, h_a = 13.2 \text{ cm}, h_b = 17.9 \text{ cm}, h_c = 8.3 \text{ cm}, u = 79.2 \text{ cm}, A = 157.4 \text{ cm}^2$
11	$b = 16.1 \text{ cm}, c = 17.3 \text{ cm}, h_a = 13.9 \text{ cm}, A = 128 \text{ cm}^2$	$a = 18.4 \text{ cm}, b = 16.1 \text{ cm}, c = 17.3 \text{ cm}, h_a = 13.9 \text{ cm}, h_b = 15.9 \text{ cm}, h_c = 14.8 \text{ cm}, u = 51.8 \text{ cm}, A = 128 \text{ cm}^2$
12	$a = 10.6 \text{ cm}, c = 22.7 \text{ cm}, h_b = 10.6 \text{ cm}, A = 101.4 \text{ cm}^2$	$a = 10.6 \text{ cm}, b = 19.2 \text{ cm}, c = 22.7 \text{ cm}, h_a = 19.1 \text{ cm}, h_b = 10.6 \text{ cm}, h_c = 8.9 \text{ cm}, u = 52.5 \text{ cm}, A = 101.4 \text{ cm}^2$
13	$b = 11.4 \text{ cm}, c = 13.4 \text{ cm}, h_a = 6.4 \text{ cm}, A = 67.9 \text{ cm}^2$	$a = 21.2 \text{ cm}, b = 11.4 \text{ cm}, c = 13.4 \text{ cm}, h_a = 6.4 \text{ cm}, h_b = 11.9 \text{ cm}, h_c = 10.1 \text{ cm}, u = 46 \text{ cm}, A = 67.9 \text{ cm}^2$
14	$a = 14.7 \text{ cm}, c = 12.2 \text{ cm}, h_b = 10.6 \text{ cm}, A = 86.2 \text{ cm}^2$	$a = 14.7 \text{ cm}, b = 16.3 \text{ cm}, c = 12.2 \text{ cm}, h_a = 11.7 \text{ cm}, h_b = 10.6 \text{ cm}, h_c = 14.1 \text{ cm}, u = 43.2 \text{ cm}, A = 86.2 \text{ cm}^2$
15	$a = 11.2 \text{ cm}, c = 15 \text{ cm}, h_b = 11 \text{ cm}, A = 69 \text{ cm}^2$	$a = 11.2 \text{ cm}, b = 12.6 \text{ cm}, c = 15 \text{ cm}, h_a = 12.3 \text{ cm}, h_b = 11 \text{ cm}, h_c = 9.2 \text{ cm}, u = 38.8 \text{ cm}, A = 69 \text{ cm}^2$
16	$b = 8.7 \text{ cm}, c = 11.4 \text{ cm}, h_a = 5.7 \text{ cm}, A = 47 \text{ cm}^2$	$a = 16.4 \text{ cm}, b = 8.7 \text{ cm}, c = 11.4 \text{ cm}, h_a = 5.7 \text{ cm}, h_b = 10.8 \text{ cm}, h_c = 8.2 \text{ cm}, u = 36.5 \text{ cm}, A = 47 \text{ cm}^2$
17	$b = 10.4 \text{ cm}, c = 10.2 \text{ cm}, h_a = 7.3 \text{ cm}, A = 53 \text{ cm}^2$	$a = 14.6 \text{ cm}, b = 10.4 \text{ cm}, c = 10.2 \text{ cm}, h_a = 7.3 \text{ cm}, h_b = 10.2 \text{ cm}, h_c = 10.4 \text{ cm}, u = 35.2 \text{ cm}, A = 53 \text{ cm}^2$
18	$b = 13.7 \text{ cm}, c = 18.4 \text{ cm}, h_a = 9.2 \text{ cm}, A = 26.8 \text{ cm}^2$	$a = 5.8 \text{ cm}, b = 13.7 \text{ cm}, c = 18.4 \text{ cm}, h_a = 9.2 \text{ cm}, h_b = 3.9 \text{ cm}, h_c = 2.9 \text{ cm}, u = 37.9 \text{ cm}, A = 26.8 \text{ cm}^2$
19	$a = 19.6 \text{ cm}, c = 29.9 \text{ cm}, h_b = 19.3 \text{ cm}, A = 184.8 \text{ cm}^2$	$a = 19.6 \text{ cm}, b = 19.2 \text{ cm}, c = 29.9 \text{ cm}, h_a = 18.9 \text{ cm}, h_b = 19.3 \text{ cm}, h_c = 12.4 \text{ cm}, u = 68.7 \text{ cm}, A = 184.8 \text{ cm}^2$
20	$a = 13.9 \text{ cm}, b = 7.3 \text{ cm}, h_c = 6.3 \text{ cm}, A = 50.6 \text{ cm}^2$	$a = 13.9 \text{ cm}, b = 7.3 \text{ cm}, c = 16.1 \text{ cm}, h_a = 7.3 \text{ cm}, h_b = 13.9 \text{ cm}, h_c = 6.3 \text{ cm}, u = 37.3 \text{ cm}, A = 50.6 \text{ cm}^2$

**Aufgabe 8:** Berechne die fehlende Seite, die fehlenden Höhen und den Umfang des allgemeinen Dreiecks (Seiten  $a, b, c$ , Höhen  $h_a, h_b, h_c$ ,  $u$  = Umfang,  $A$  = Flächeninhalt).

Nr.	Gegeben:
1	$a = 7.5 \text{ cm}, c = 25 \text{ cm}, h_b = 7.4 \text{ cm}, A = 83.5 \text{ cm}^2$
2	$a = 24.4 \text{ m}, b = 18.8 \text{ m}, h_c = 17.5 \text{ m}, A = 89.5 \text{ m}^2$
3	$a = 13.8 \text{ mm}, b = 16.2 \text{ mm}, h_c = 5.1 \text{ mm}, A = 71.9 \text{ mm}^2$
4	$b = 18.4 \text{ m}, c = 27.9 \text{ m}, h_a = 17.8 \text{ m}, A = 148.3 \text{ m}^2$

5	$a = 24.5 \text{ cm}, b = 13.1 \text{ cm}, h_c = 8.9 \text{ cm}, A = 58.6 \text{ cm}^2$
6	$a = 8.3 \text{ m}, c = 4 \text{ m}, h_b = 3.5 \text{ m}, A = 9.8 \text{ m}^2$
7	$a = 9.5 \text{ cm}, c = 21 \text{ cm}, h_b = 8.6 \text{ cm}, A = 99.7 \text{ cm}^2$
8	$a = 15.1 \text{ cm}, b = 23.4 \text{ cm}, h_c = 12.7 \text{ cm}, A = 73.1 \text{ cm}^2$
9	$a = 11.8 \text{ mm}, b = 24.4 \text{ mm}, h_c = 10.9 \text{ mm}, A = 95.2 \text{ mm}^2$
10	$b = 19.9 \text{ mm}, c = 11.7 \text{ mm}, h_a = 11.5 \text{ mm}, A = 104.9 \text{ mm}^2$
11	$b = 9 \text{ dm}, c = 27.7 \text{ dm}, h_a = 8.6 \text{ dm}, A = 102.8 \text{ dm}^2$
12	$b = 9.4 \text{ m}, c = 12.6 \text{ m}, h_a = 7.4 \text{ m}, A = 59.2 \text{ m}^2$
13	$a = 11.1 \text{ m}, b = 12.8 \text{ m}, h_c = 11 \text{ m}, A = 28.7 \text{ m}^2$
14	$b = 21.9 \text{ dm}, c = 28.4 \text{ dm}, h_a = 11.3 \text{ dm}, A = 41.3 \text{ dm}^2$
15	$b = 14.3 \text{ dm}, c = 6.7 \text{ dm}, h_a = 6.1 \text{ dm}, A = 47.9 \text{ dm}^2$
16	$a = 8 \text{ m}, c = 23.3 \text{ m}, h_b = 8 \text{ m}, A = 84 \text{ m}^2$
17	$b = 10.7 \text{ m}, c = 6.5 \text{ m}, h_a = 3.7 \text{ m}, A = 8.7 \text{ m}^2$
18	$a = 22.4 \text{ cm}, c = 29.9 \text{ cm}, h_b = 22.4 \text{ cm}, A = 212.7 \text{ cm}^2$
19	$b = 10.5 \text{ mm}, c = 10.5 \text{ mm}, h_a = 9.8 \text{ mm}, A = 37.2 \text{ mm}^2$
20	$a = 7.9 \text{ dm}, b = 22.2 \text{ dm}, h_c = 7.8 \text{ dm}, A = 85.4 \text{ dm}^2$

**Vorgehensweise:** Zur Ermittlung der fehlenden Größen beim allgemeinen Dreieck ist die obige Formelsammlung anzuwenden.

**Lösungen:**

Nr.	Gegeben:	Lösungen:
1	$a = 7.5 \text{ cm}, c = 25 \text{ cm}, h_b = 7.4 \text{ cm}, A = 83.5 \text{ cm}^2$	$a = 7.5 \text{ cm}, b = 22.6 \text{ cm}, c = 25 \text{ cm}, h_a = 22.3 \text{ cm}, h_b = 7.4 \text{ cm}, h_c = 6.7 \text{ cm}, u = 55.1 \text{ cm}, A = 83.5 \text{ cm}^2$
2	$a = 24.4 \text{ m}, b = 18.8 \text{ m}, h_c = 17.5 \text{ m}, A = 89.5 \text{ m}^2$	$a = 24.4 \text{ m}, b = 18.8 \text{ m}, c = 10.2 \text{ m}, h_a = 7.3 \text{ m}, h_b = 9.5 \text{ m}, h_c = 17.5 \text{ m}, u = 53.4 \text{ m}, A = 89.5 \text{ m}^2$
3	$a = 13.8 \text{ mm}, b = 16.2 \text{ mm}, h_c = 5.1 \text{ mm}, A = 71.9 \text{ mm}^2$	$a = 13.8 \text{ mm}, b = 16.2 \text{ mm}, c = 28.2 \text{ mm}, h_a = 10.4 \text{ mm}, h_b = 8.9 \text{ mm}, h_c = 5.1 \text{ mm}, u = 58.2 \text{ mm}, A = 71.9 \text{ mm}^2$
4	$b = 18.4 \text{ m}, c = 27.9 \text{ m}, h_a = 17.8 \text{ m}, A = 148.3 \text{ m}^2$	$a = 16.7 \text{ m}, b = 18.4 \text{ m}, c = 27.9 \text{ m}, h_a = 17.8 \text{ m}, h_b = 16.1 \text{ m}, h_c = 10.6 \text{ m}, u = 63 \text{ m}, A = 148.3 \text{ m}^2$
5	$a = 24.5 \text{ cm}, b = 13.1 \text{ cm}, h_c = 8.9 \text{ cm}, A = 58.6 \text{ cm}^2$	$a = 24.5 \text{ cm}, b = 13.1 \text{ cm}, c = 13.2 \text{ cm}, h_a = 4.8 \text{ cm}, h_b = 8.9 \text{ cm}, h_c = 8.9 \text{ cm}, u = 50.8 \text{ cm}, A = 58.6 \text{ cm}^2$
6	$a = 8.3 \text{ m}, c = 4 \text{ m}, h_b = 3.5 \text{ m}, A = 9.8 \text{ m}^2$	$a = 8.3 \text{ m}, b = 5.6 \text{ m}, c = 4 \text{ m}, h_a = 2.4 \text{ m}, h_b = 3.5 \text{ m}, h_c = 4.9 \text{ m}, u = 17.9 \text{ m}, A = 9.8 \text{ m}^2$
7	$a = 9.5 \text{ cm}, c = 21 \text{ cm}, h_b = 8.6 \text{ cm}, A = 99.7 \text{ cm}^2$	$a = 9.5 \text{ cm}, b = 23.3 \text{ cm}, c = 21 \text{ cm}, h_a = 21 \text{ cm}, h_b = 8.6 \text{ cm}, h_c = 9.5 \text{ cm}, u = 53.8 \text{ cm}, A = 99.7 \text{ cm}^2$
8	$a = 15.1 \text{ cm}, b = 23.4 \text{ cm}, h_c = 12.7 \text{ cm}, A = 73.1 \text{ cm}^2$	$a = 15.1 \text{ cm}, b = 23.4 \text{ cm}, c = 11.5 \text{ cm}, h_a = 9.7 \text{ cm}, h_b = 6.2 \text{ cm}, h_c = 12.7 \text{ cm}, u = 50 \text{ cm}, A = 73.1 \text{ cm}^2$
9	$a = 11.8 \text{ mm}, b = 24.4 \text{ mm}, h_c = 10.9 \text{ mm}, A = 95.2 \text{ mm}^2$	$a = 11.8 \text{ mm}, b = 24.4 \text{ mm}, c = 17.4 \text{ mm}, h_a = 16.1 \text{ mm}, h_b = 7.8 \text{ mm}, h_c = 10.9 \text{ mm}, u = 53.6 \text{ mm}, A = 95.2 \text{ mm}^2$
10	$b = 19.9 \text{ mm}, c = 11.7 \text{ mm}, h_a = 11.5 \text{ mm}, A = 104.9 \text{ mm}^2$	$a = 18.2 \text{ mm}, b = 19.9 \text{ mm}, c = 11.7 \text{ mm}, h_a = 11.5 \text{ mm}, h_b = 10.5 \text{ mm}, h_c = 17.9 \text{ mm}, u = 49.8 \text{ mm}, A = 104.9 \text{ mm}^2$
11	$b = 9 \text{ dm}, c = 27.7 \text{ dm}, h_a = 8.6 \text{ dm}, A = 102.8 \text{ dm}^2$	$a = 23.8 \text{ dm}, b = 9 \text{ dm}, c = 27.7 \text{ dm}, h_a = 8.6 \text{ dm}, h_b = 22.8 \text{ dm}, h_c = 7.4 \text{ dm}, u = 60.5 \text{ dm}, A = 102.8 \text{ dm}^2$
12	$b = 9.4 \text{ m}, c = 12.6 \text{ m}, h_a = 7.4 \text{ m}, A = 59.2 \text{ m}^2$	$a = 15.9 \text{ m}, b = 9.4 \text{ m}, c = 12.6 \text{ m}, h_a = 7.4 \text{ m}, h_b = 12.6 \text{ m}, h_c = 9.4 \text{ m}, u = 37.9 \text{ m}, A = 59.2 \text{ m}^2$
13	$a = 11.1 \text{ m}, b = 12.8 \text{ m}, h_c = 11 \text{ m}, A = 28.7 \text{ m}^2$	$a = 11.1 \text{ m}, b = 12.8 \text{ m}, c = 5.2 \text{ m}, h_a = 5.2 \text{ m}, h_b = 4.5 \text{ m}, h_c = 11 \text{ m}, u = 29.1 \text{ m}, A = 28.7 \text{ m}^2$
14	$b = 21.9 \text{ dm}, c = 28.4 \text{ dm}, h_a = 11.3 \text{ dm}, A = 41.3 \text{ dm}^2$	$a = 7.3 \text{ dm}, b = 21.9 \text{ dm}, c = 28.4 \text{ dm}, h_a = 11.3 \text{ dm}, h_b = 3.8 \text{ dm}, h_c = 2.9 \text{ dm}, u = 57.6 \text{ dm}, A = 41.3 \text{ dm}^2$

15	$b = 14.3 \text{ dm}, c = 6.7 \text{ dm}, h_a = 6.1 \text{ dm}, A = 47.9 \text{ dm}^2$	$a = 15.7 \text{ dm}, b = 14.3 \text{ dm}, c = 6.7 \text{ dm}, h_a = 6.1 \text{ dm}, h_b = 6.7 \text{ dm}, h_c = 14.3 \text{ dm}, u = 36.7 \text{ dm}, A = 47.9 \text{ dm}^2$
16	$a = 8 \text{ m}, c = 23.3 \text{ m}, h_b = 8 \text{ m}, A = 84 \text{ m}^2$	$a = 8 \text{ m}, b = 21.1 \text{ m}, c = 23.3 \text{ m}, h_a = 21 \text{ m}, h_b = 8 \text{ m}, h_c = 7.2 \text{ m}, u = 52.4 \text{ m}, A = 84 \text{ m}^2$
17	$b = 10.7 \text{ m}, c = 6.5 \text{ m}, h_a = 3.7 \text{ m}, A = 8.7 \text{ m}^2$	$a = 4.7 \text{ m}, b = 10.7 \text{ m}, c = 6.5 \text{ m}, h_a = 3.7 \text{ m}, h_b = 1.6 \text{ m}, h_c = 2.7 \text{ m}, u = 21.9 \text{ m}, A = 8.7 \text{ m}^2$
18	$a = 22.4 \text{ cm}, c = 29.9 \text{ cm}, h_b = 22.4 \text{ cm}, A = 212.7 \text{ cm}^2$	$a = 22.4 \text{ cm}, b = 19 \text{ cm}, c = 29.9 \text{ cm}, h_a = 19 \text{ cm}, h_b = 22.4 \text{ cm}, h_c = 14.2 \text{ cm}, u = 71.3 \text{ cm}, A = 212.7 \text{ cm}^2$
19	$b = 10.5 \text{ mm}, c = 10.5 \text{ mm}, h_a = 9.8 \text{ mm}, A = 37.2 \text{ mm}^2$	$a = 7.6 \text{ mm}, b = 10.5 \text{ mm}, c = 10.5 \text{ mm}, h_a = 9.8 \text{ mm}, h_b = 7.1 \text{ mm}, h_c = 7.1 \text{ mm}, u = 28.6 \text{ mm}, A = 37.2 \text{ mm}^2$
20	$a = 7.9 \text{ dm}, b = 22.2 \text{ dm}, h_c = 7.8 \text{ dm}, A = 85.4 \text{ dm}^2$	$a = 7.9 \text{ dm}, b = 22.2 \text{ dm}, c = 21.8 \text{ dm}, h_a = 21.6 \text{ dm}, h_b = 7.7 \text{ dm}, h_c = 7.8 \text{ dm}, u = 51.9 \text{ dm}, A = 85.4 \text{ dm}^2$

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