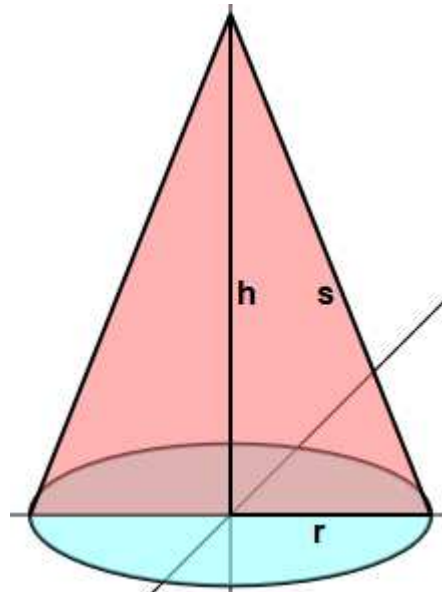


Mathematik-Aufgabenpool

> Kegelberechnung I

Einleitung: Ein (gerader) Kegel mit einem Kreis als Grundfläche ist durch den Radius r des Kreises mit Durchmesser d und Kreisumfang u sowie durch die Kegelhöhe h bestimmt, weiter durch die Mantellinie s , durch die Grundfläche G , die Oberfläche O , die Mantelfläche M und das Volumen V . Es gilt: $d=2r$, $u=2\pi r$, $s=\sqrt{r^2 + h^2}$, $G=\pi r^2$, $M=\pi r s$, $O=G+M$, $V=Gh/3$.



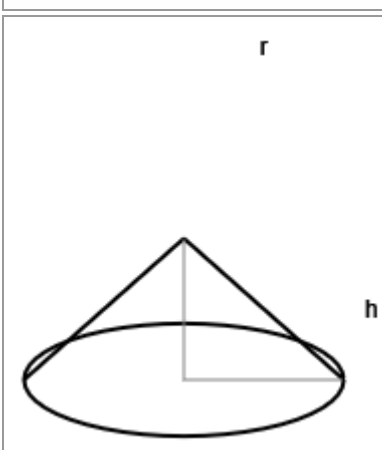
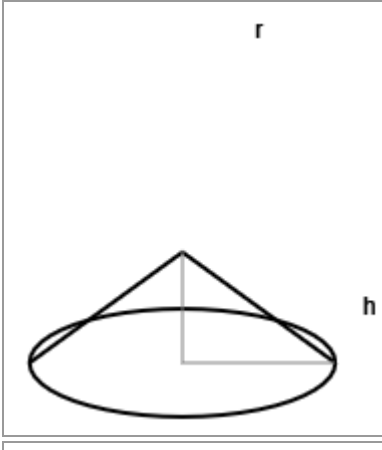
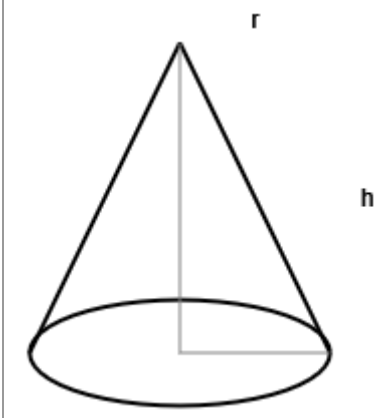
Kegel: Radius r , Höhe h , Mantellinie s

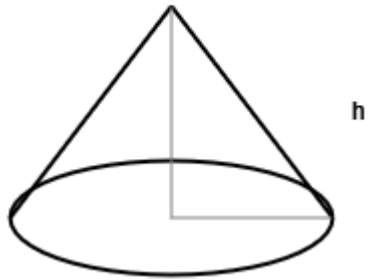
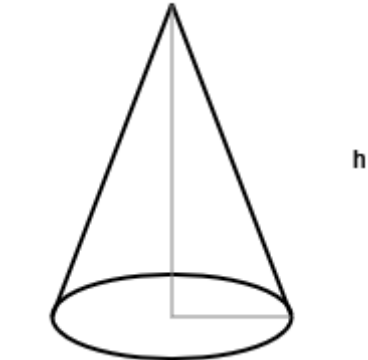


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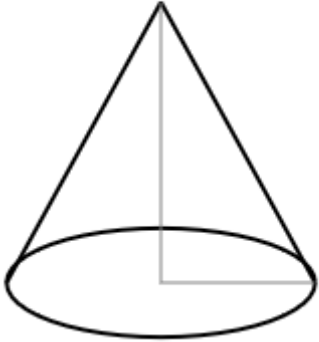
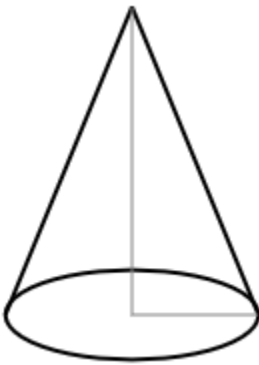

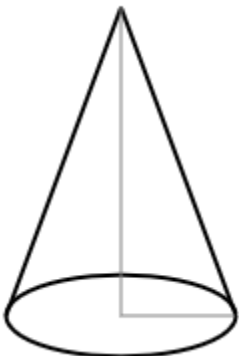
Grundfläche, Radius	$G = \pi r^2$	$r = \sqrt{\frac{G}{\pi}}$	
Durchmesser	$d = 2r$	$r = \frac{d}{2}$	
Kreisumfang	$U = 2\pi r$	$U = \pi d$	$r = \frac{U}{2\pi}$
Mantellinie, Höhe	$s^2 = r^2 + h^2$	$r^2 = s^2 - h^2$	$h^2 = s^2 - r^2$
Mantelfläche	$M = \pi r s$	$r = \frac{M}{\pi s}$	$s = \frac{M}{\pi r}$
Oberfläche	$O = G + M = \pi r^2 + \pi r s = \pi r(r + s)$		
	$G = O - M$	$M = O - G$	
		$r = -\frac{s}{2} + \sqrt{\frac{s^2}{4} + \frac{O}{\pi}}$	$s = \frac{O}{\pi r} - r$
Volumen	$V = \frac{1}{3} G \cdot h = \frac{1}{3} \pi r^2 h$	$r = \sqrt{\frac{3V}{\pi h}}$	$h = \frac{3V}{\pi r^2}$
Winkel zwischen Mantel- und Grundfläche	$\sin \alpha = \frac{h}{s}$	$\cos \alpha = \frac{r}{s}$	$\tan \alpha = \frac{h}{r}$

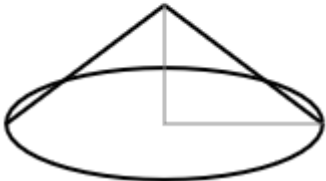
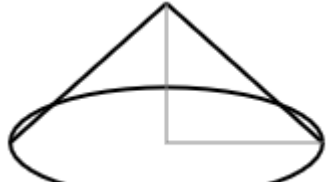
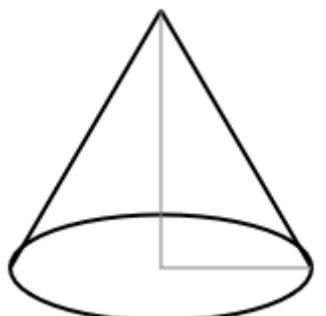
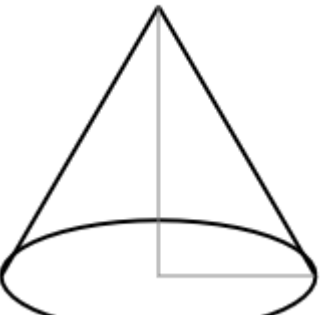
Halber Winkel in der Kegelspitze	$\sin \beta = \frac{r}{s}$	$\cos \beta = \frac{h}{s}$	$\tan \beta = \frac{r}{h}$
Kreisbogen	$b = 2\pi r$	$b = \pi s \cdot \frac{\gamma}{180^\circ}$	$s = b \cdot \frac{180^\circ}{\pi \cdot \gamma}$
Abrollfläche, Kreisausschnitt	$A = M = \pi r s$	$A = \pi s^2 \cdot \frac{\gamma}{360^\circ}$	
Abrollwinkel	$\gamma = \frac{b}{\pi s} \cdot 180^\circ$	$\gamma = \frac{A}{\pi s^2} \cdot 360^\circ$	$\gamma = \frac{r}{s} \cdot 360^\circ$

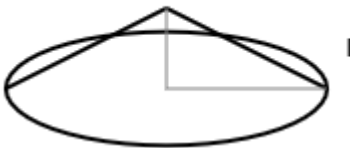
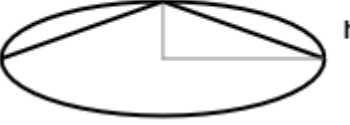
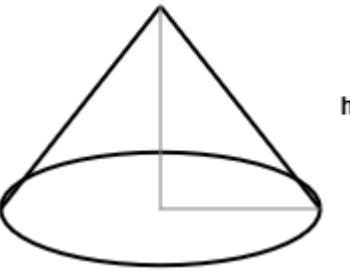
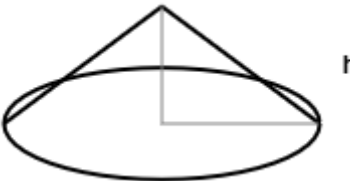
Aufgabe 1: Bestimme mit vorgegebenem Radius r und vorgegebener Höhe h den Durchmesser d, den Umfang u, die Mantellinie s, die Grundfläche G, die Mantelfläche M, die Oberfläche O und das Volumen V des Kegels.


Nr.	Gegeben:	Gesucht:	Grafik:
1	r = 13.3 cm, h = 11.8 cm	d, u, G, s, M, O, V	
2	r = 10.5 cm, h = 7.6 cm	d, u, G, s, M, O, V	
3	r = 7.2 cm, h = 14.9 cm	d, u, G, s, M, O, V	

4	$r = 14.4 \text{ cm}$, $h = 18.9 \text{ cm}$	d, u, G, s, M, O, V	
5	$r = 7.5 \text{ cm}$, $h = 19.6 \text{ cm}$	d, u, G, s, M, O, V	
6	$r = 3.8 \text{ cm}$, $h = 12.0 \text{ cm}$	d, u, G, s, M, O, V	
7	$r = 14.6 \text{ cm}$, $h = 13.8 \text{ cm}$	d, u, G, s, M, O, V	

8	$r = 8.3 \text{ cm}, h = 15.1 \text{ cm}$	d, u, G, s, M, O, V	 <p>A diagram of a cone. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'.</p>
9	$r = 6.1 \text{ cm}, h = 14.8 \text{ cm}$	d, u, G, s, M, O, V	 <p>A diagram of a cone. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'.</p>
10	$r = 2.7 \text{ cm}, h = 6.4 \text{ cm}$	d, u, G, s, M, O, V	 <p>A diagram of a cone. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'.</p>
11	$r = 6.9 \text{ cm}, h = 18.4 \text{ cm}$	d, u, G, s, M, O, V	 <p>A diagram of a cone. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'.</p>

12	$r = 13.2 \text{ cm}$, $h = 9.9 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 
13	$r = 13.5 \text{ cm}$, $h = 12.0 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 
14	$r = 9.0 \text{ cm}$, $h = 15.4 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 
15	$r = 10.8 \text{ cm}$, $h = 18.5 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 

16	$r = 13.4 \text{ cm}$, $h = 6.7 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 
17	$r = 14.4 \text{ cm}$, $h = 5.1 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 
18	$r = 13.8 \text{ cm}$, $h = 17.5 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 
19	$r = 13.6 \text{ cm}$, $h = 10.1 \text{ cm}$	d, u, G, s, M, O, V	<p style="text-align: center;">r</p> 

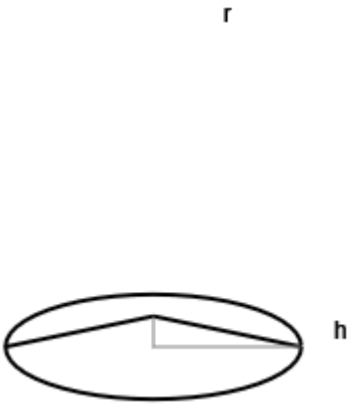
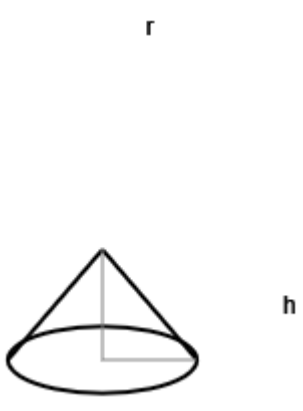
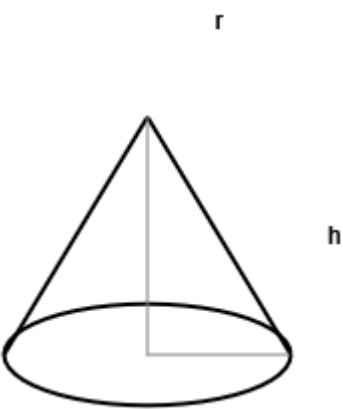
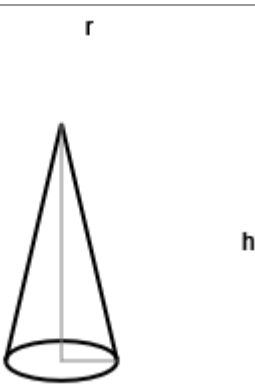
20	$r = 4.7 \text{ cm}, h = 9.7 \text{ cm}$	d, u, G, s, M, O, V	
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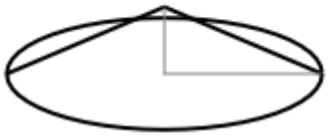
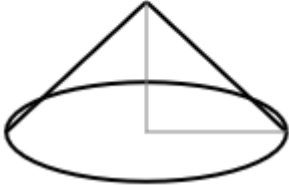
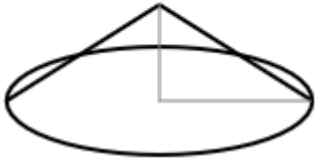
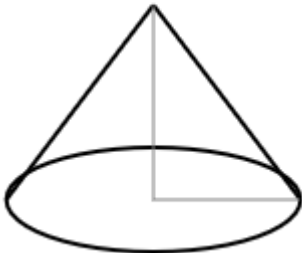
Vorgehensweise: Zur Ermittlung der fehlenden Größen beim Kegel ist die obige Formelsammlung anzuwenden.

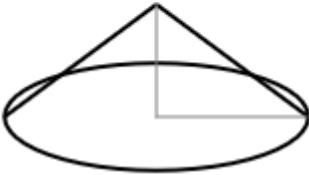
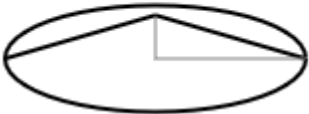
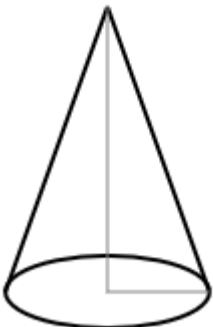
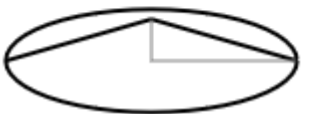
Lösungen:

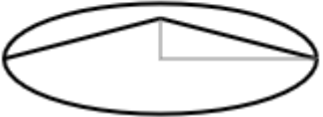
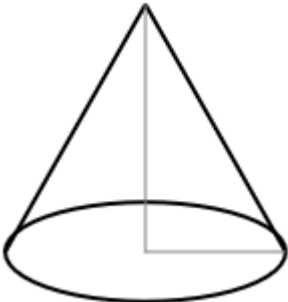
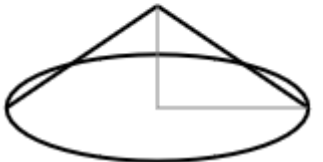
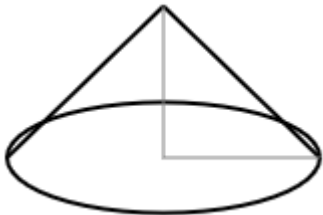
Nr.	r=	d=	u=	G=	h=	s=	M=	O=	V=
1	13.3 cm	26.6 cm	83.6 cm	555.7 cm ²	11.8 cm	17.8 cm	743.7 cm ²	1299.4 cm ²	2185.8 cm ³
2	10.5 cm	21.0 cm	66.0 cm	346.4 cm ²	7.6 cm	13.0 cm	428.8 cm ²	775.2 cm ²	877.4 cm ³
3	7.2 cm	14.4 cm	45.2 cm	162.9 cm ²	14.9 cm	16.5 cm	373.2 cm ²	536.1 cm ²	808.9 cm ³
4	14.4 cm	28.8 cm	90.5 cm	651.4 cm ²	18.9 cm	23.8 cm	1076.7 cm ²	1728.1 cm ²	4104.1 cm ³
5	7.5 cm	15.0 cm	47.1 cm	176.7 cm ²	19.6 cm	21.0 cm	494.8 cm ²	671.5 cm ²	1154.5 cm ³
6	3.8 cm	7.6 cm	23.9 cm	45.4 cm ²	12.0 cm	12.6 cm	150.4 cm ²	195.8 cm ²	181.5 cm ³
7	14.6 cm	29.2 cm	91.7 cm	669.7 cm ²	13.8 cm	20.1 cm	921.9 cm ²	1591.6 cm ²	3080.4 cm ³
8	8.3 cm	16.6 cm	52.2 cm	216.4 cm ²	15.1 cm	17.2 cm	448.5 cm ²	664.9 cm ²	1089.3 cm ³
9	6.1 cm	12.2 cm	38.3 cm	116.9 cm ²	14.8 cm	16.0 cm	306.6 cm ²	423.5 cm ²	576.7 cm ³
10	2.7 cm	5.4 cm	17.0 cm	22.9 cm ²	6.4 cm	6.9 cm	58.8 cm ²	81.4 cm ²	48.9 cm ³
11	6.9 cm	13.8 cm	43.4 cm	149.6 cm ²	18.4 cm	19.7 cm	427.0 cm ²	576.6 cm ²	917.4 cm ³
12	13.2 cm	26.4 cm	82.9 cm	547.4 cm ²	9.9 cm	16.5 cm	684.2 cm ²	1231.6 cm ²	1806.4 cm ³
13	13.5 cm	27.0 cm	84.8 cm	572.6 cm ²	12.0 cm	18.1 cm	767.6 cm ²	1340.2 cm ²	2290.2 cm ³
14	9.0 cm	18.0 cm	56.5 cm	254.5 cm ²	15.4 cm	17.8 cm	503.3 cm ²	757.8 cm ²	1306.3 cm ³
15	10.8 cm	21.6 cm	67.9 cm	366.4 cm ²	18.5 cm	21.4 cm	726.1 cm ²	1092.5 cm ²	2259.7 cm ³
16	13.4 cm	26.8 cm	84.2 cm	564.1 cm ²	6.7 cm	15.0 cm	631.5 cm ²	1195.6 cm ²	1259.8 cm ³
17	14.4 cm	28.8 cm	90.5 cm	651.4 cm ²	5.1 cm	15.3 cm	692.2 cm ²	1343.6 cm ²	1107.4 cm ³
18	13.8 cm	27.6 cm	86.7 cm	598.3 cm ²	17.5 cm	22.3 cm	966.8 cm ²	1565.1 cm ²	3490.0 cm ³
19	13.6 cm	27.2 cm	85.5 cm	581.1 cm ²	10.1 cm	16.9 cm	722.1 cm ²	1302.2 cm ²	1956.3 cm ³
20	4.7 cm	9.4 cm	29.5 cm	69.4 cm ²	9.7 cm	10.8 cm	159.5 cm ²	228.9 cm ²	224.4 cm ³



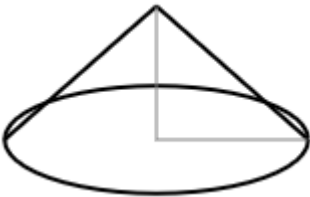
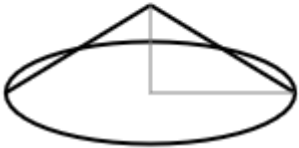
Aufgabe 2: Bestimme die fehlenden Größen (Radius r , Durchmesser d , Umfang u , Mantellinie s , Grundfläche G , Mantelfläche M , Oberfläche O , Volumen V) des Kegels.

Nr.	Gegeben:	Gesucht:	Grafik:
1	$h = 1.2 \text{ cm}$, $O = 320.7 \text{ cm}^2$	r , d , u , G , s , M , V	 <p>A diagram of a cone shown from a perspective view. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'. The base is an ellipse.</p>
2	$u = 7.5 \text{ cm}$, $s = 1.8 \text{ cm}$	r , d , G , h , M , O , V	 <p>A diagram of a cone shown from a perspective view. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'. The base is an ellipse.</p>
3	$d = 10.4 \text{ cm}$, $O = 411.6 \text{ cm}^2$	r , u , G , h , s , M , V	 <p>A diagram of a cone shown from a perspective view. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'. The base is an ellipse.</p>
4	$d = 2.4 \text{ cm}$, $s = 5.2 \text{ cm}$	r , u , G , h , M , O , V	 <p>A diagram of a cone shown from a perspective view. A vertical line segment from the apex to the center of the base is labeled 'h'. A horizontal line segment from the center of the base to the edge is labeled 'r'. The base is an ellipse.</p>

5	$d = 19.8 \text{ cm}, V = 431.1 \text{ cm}^3$	r, u, G, h, s, M, O	<p style="text-align: center;">r</p> 
6	$G = 95.0 \text{ cm}^2, O = 354.2 \text{ cm}^2$	r, d, u, h, s, M, V	<p style="text-align: center;">r</p> 
7	$u = 49.0 \text{ cm}, h = 4.9 \text{ cm}$	r, d, G, s, M, O, V	<p style="text-align: center;">r</p> 
8	$u = 47.1 \text{ cm}, M = 584.3 \text{ cm}^2$	r, d, G, h, s, O, V	<p style="text-align: center;">r</p> 

9	$r = 7.3 \text{ cm}, s = 9.1 \text{ cm}$	d, u, G, h, M, O, V	<p style="text-align: center;">r</p> 
10	$u = 37.1 \text{ cm}, h = 1.7 \text{ cm}$	r, d, G, s, M, O, V	<p style="text-align: center;">r</p> 
11	$u = 21.4 \text{ cm}, V = 115.0 \text{ cm}^3$	r, d, G, h, s, M, O	<p style="text-align: center;">r</p> 
12	$u = 44.0 \text{ cm}, M = 321.1 \text{ cm}^2$	r, d, G, h, s, O, V	<p style="text-align: center;">r</p> 

13	$M = 514.5 \text{ cm}^2$, $O = 763.3 \text{ cm}^2$	r, d, u, G, h, s, V	<p style="text-align: center;">r</p> 
14	$r = 5.5 \text{ cm}$, $s = 11.2 \text{ cm}$	d, u, G, h, M, O, V	<p style="text-align: center;">r</p> 
15	$r = 7.7 \text{ cm}$, $s = 9.3 \text{ cm}$	d, u, G, h, M, O, V	<p style="text-align: center;">r</p> 
16	$d = 17.8 \text{ cm}$, $s = 12.4 \text{ cm}$	r, u, G, h, M, O, V	<p style="text-align: center;">r</p> 

17	$s = 3.4 \text{ cm}$, $M = 57.7 \text{ cm}^2$	r, d, u, G, h, O, V	
18	$r = 1.1 \text{ cm}$, $s = 1.8 \text{ cm}$	d, u, G, h, M, O, V	
19	$s = 9.7 \text{ cm}$, $G = 167.4 \text{ cm}^2$	r, d, u, h, M, O, V	
20	$d = 12.2 \text{ cm}$, $s = 7.1 \text{ cm}$	r, u, G, h, M, O, V	

Vorgehensweise: Zur Ermittlung der fehlenden Größen beim Kegel ist die obige Formelsammlung anzuwenden.

Lösungen:

Nr.	r=	d=	u=	G=	h=	s=	M=	O=	V=
1	5.8 cm	11.6 cm	36.4 cm	105.7 cm ²	1.2 cm	5.9 cm	107.5 cm ²	213.2 cm ²	42.3 cm ³
2	1.2 cm	2.4 cm	7.5 cm	4.5 cm ²	1.4 cm	1.8 cm	6.8 cm ²	11.3 cm ²	2.1 cm ³

3	5.2 cm	10.4 cm	32.7 cm	84.9 cm ²	8.6 cm	10.0 cm	163.4 cm ²	248.3 cm ²	243.5 cm ³
4	1.2 cm	2.4 cm	7.5 cm	4.5 cm ²	5.1 cm	5.2 cm	19.6 cm ²	14.1 cm ²	7.7 cm ³
5	9.9 cm	19.8 cm	62.2 cm	307.9 cm ²	4.2 cm	10.8 cm	335.9 cm ²	643.8 cm ²	431.1 cm ³
6	5.5 cm	11.0 cm	34.6 cm	95.0 cm ²	5.1 cm	7.5 cm	129.6 cm ²	224.6 cm ²	161.6 cm ³
7	7.8 cm	15.6 cm	49.0 cm	191.1 cm ²	4.9 cm	9.2 cm	225.4 cm ²	416.5 cm ²	312.2 cm ³
8	7.5 cm	15.0 cm	47.1 cm	176.7 cm ²	9.9 cm	12.4 cm	292.2 cm ²	468.9 cm ²	583.2 cm ³
9	7.3 cm	14.6 cm	45.9 cm	167.4 cm ²	5.4 cm	9.1 cm	208.7 cm ²	376.1 cm ²	301.3 cm ³
10	5.9 cm	11.8 cm	37.1 cm	109.4 cm ²	1.7 cm	6.1 cm	113.1 cm ²	222.5 cm ²	62.0 cm ³
11	3.4 cm	6.8 cm	21.4 cm	36.3 cm ²	9.5 cm	10.1 cm	107.9 cm ²	144.2 cm ²	115.0 cm ³
12	7.0 cm	14.0 cm	44.0 cm	153.9 cm ²	2.0 cm	7.3 cm	160.5 cm ²	314.4 cm ²	102.6 cm ³
13	8.9 cm	17.8 cm	55.9 cm	248.8 cm ²	2.3 cm	9.2 cm	257.2 cm ²	506.0 cm ²	190.8 cm ³
14	5.5 cm	11.0 cm	34.6 cm	95.0 cm ²	9.7 cm	11.2 cm	193.5 cm ²	288.5 cm ²	307.3 cm ³
15	7.7 cm	15.4 cm	48.4 cm	186.3 cm ²	5.2 cm	9.3 cm	225.0 cm ²	411.3 cm ²	322.9 cm ³
16	8.9 cm	17.8 cm	55.9 cm	248.8 cm ²	8.6 cm	12.4 cm	346.7 cm ²	595.5 cm ²	713.4 cm ³
17	2.7 cm	5.4 cm	17.0 cm	22.9 cm ²	2.1 cm	3.4 cm	28.8 cm ²	51.7 cm ²	16.0 cm ³
18	1.1 cm	2.2 cm	6.9 cm	3.8 cm ²	1.4 cm	1.8 cm	6.2 cm ²	10.0 cm ²	1.8 cm ³
19	7.3 cm	14.6 cm	45.9 cm	167.4 cm ²	6.4 cm	9.7 cm	222.5 cm ²	389.9 cm ²	357.2 cm ³
20	6.1 cm	12.2 cm	38.3 cm	116.9 cm ²	3.7 cm	7.1 cm	136.1 cm ²	253.0 cm ²	144.2 cm ³

Aufgabe 3: Bestimme die fehlenden Größen (Radius r, Durchmesser d, Umfang u, Mantellinie s, Grundfläche G, Mantelfläche M, Oberfläche O, Volumen V) des Kegels.

Nr.	Gegeben:	Gesucht:
1	$M = 158.8 \text{ dm}^2, V = 197.3 \text{ dm}^3$	r, d, u, G, h, s, O
2	$d = 14.2 \text{ mm}, s = 7.2 \text{ mm}$	r, u, G, h, M, O, V
3	$s = 9.2 \text{ cm}, O = 393.5 \text{ cm}^2$	r, d, u, G, h, M, V
4	$d = 18.2 \text{ dm}, h = 9.7 \text{ dm}$	r, u, G, s, M, O, V
5	$h = 9.4 \text{ mm}, M = 426.1 \text{ mm}^2$	r, d, u, G, s, O, V
6	$M = 242.6 \text{ mm}^2, V = 442.5 \text{ mm}^3$	r, d, u, G, h, s, O
7	$r = 3.2 \text{ m}, M = 60.3 \text{ m}^2$	d, u, G, h, s, O, V
8	$d = 6.4 \text{ m}, s = 9.9 \text{ m}$	r, u, G, h, M, O, V
9	$h = 3.9 \text{ cm}, O = 55.7 \text{ cm}^2$	r, d, u, G, s, M, V
10	$u = 57.2 \text{ cm}, h = 8.6 \text{ cm}$	r, d, G, s, M, O, V
11	$G = 109.4 \text{ m}^2, V = 153.1 \text{ m}^3$	r, d, u, h, s, M, O
12	$h = 7.4 \text{ mm}, M = 118.9 \text{ mm}^2$	r, d, u, G, s, O, V
13	$r = 6.6 \text{ dm}, s = 6.8 \text{ dm}$	d, u, G, h, M, O, V
14	$r = 8.1 \text{ cm}, s = 10.8 \text{ cm}$	d, u, G, h, M, O, V
15	$u = 17.6 \text{ dm}, h = 4.1 \text{ dm}$	r, d, G, s, M, O, V
16	$u = 34.6 \text{ dm}, O = 267.8 \text{ dm}^2$	r, d, G, h, s, M, V
17	$M = 48.1 \text{ m}^2, O = 57.2 \text{ m}^2$	r, d, u, G, h, s, V
18	$d = 5.2 \text{ dm}, V = 48.1 \text{ dm}^3$	r, u, G, h, s, M, O
19	$s = 9.0 \text{ cm}, M = 197.9 \text{ cm}^2$	r, d, u, G, h, O, V

20	$r = 7.8 \text{ m}, h = 6.0 \text{ m}$	d, u, G, s, M, O, V
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Vorgehensweise: Zur Ermittlung der fehlenden Größen beim Kegel ist die obige Formelsammlung anzuwenden.

Lösungen:

Nr.	r=	d=	u=	G=	h=	s=	M=	O=	V=
1	6.4 dm	12.8 dm	40.2 dm	128.7 dm ²	4.6 dm	7.9 dm	158.8 dm ²	287.5 dm ²	197.3 dm ³
2	7.1 mm	14.2 mm	44.6 mm	158.4 mm ²	1.4 mm	7.2 mm	160.6 mm ²	319.0 mm ²	73.9 mm ³
3	7.5 cm	15.0 cm	47.1 cm	176.7 cm ²	5.4 cm	9.2 cm	216.8 cm ²	393.5 cm ²	318.1 cm ³
4	9.1 dm	18.2 dm	57.2 dm	260.2 dm ²	9.7 dm	13.3 dm	380.2 dm ²	640.4 dm ²	841.2 dm ³
5	9.9 mm	19.8 mm	62.2 mm	307.9 mm ²	9.4 mm	13.7 mm	426.1 mm ²	734.0 mm ²	964.8 mm ³
6	6.6 mm	13.2 mm	41.5 mm	136.8 mm ²	9.7 mm	11.7 mm	242.6 mm ²	379.4 mm ²	442.5 mm ³
7	3.2 m	6.4 m	20.1 m	32.2 m ²	5.1 m	6.0 m	60.3 m ²	92.5 m ²	54.7 m ³
8	3.2 m	6.4 m	20.1 m	32.2 m ²	9.4 m	9.9 m	99.5 m ²	131.7 m ²	100.8 m ³
9	2.5 cm	5.0 cm	15.7 cm	19.6 cm ²	3.9 cm	4.6 cm	36.1 cm ²	55.7 cm ²	25.5 cm ³
10	9.1 cm	18.2 cm	57.2 cm	260.2 cm ²	8.6 cm	12.5 cm	357.4 cm ²	617.6 cm ²	745.8 cm ³
11	5.9 m	11.8 m	37.1 m	109.4 m ²	4.2 m	7.2 m	133.5 m ²	242.9 m ²	153.1 m ³
12	4.4 mm	8.8 mm	27.6 mm	60.8 mm ²	7.4 mm	8.6 mm	118.9 mm ²	179.7 mm ²	150.0 mm ³
13	6.6 dm	13.2 dm	41.5 dm	136.8 dm ²	1.8 dm	6.8 dm	141.0 dm ²	277.8 dm ²	82.1 dm ³
14	8.1 cm	16.2 cm	50.9 cm	206.1 cm ²	7.1 cm	10.8 cm	274.8 cm ²	480.9 cm ²	487.8 cm ³
15	2.8 dm	5.6 dm	17.6 dm	24.6 dm ²	4.1 dm	5.0 dm	44.0 dm ²	68.6 dm ²	33.7 dm ³
16	5.5 dm	11.0 dm	34.6 dm	95.0 dm ²	8.3 dm	10.0 dm	172.8 dm ²	267.8 dm ²	262.9 dm ³
17	1.7 m	3.4 m	10.7 m	9.1 m ²	8.8 m	9.0 m	48.1 m ²	57.2 m ²	26.6 m ³
18	2.6 dm	5.2 dm	16.3 dm	21.2 dm ²	6.8 dm	7.3 dm	59.6 dm ²	80.8 dm ²	48.1 dm ³
19	7.0 cm	14.0 cm	44.0 cm	153.9 cm ²	5.7 cm	9.0 cm	197.9 cm ²	351.8 cm ²	292.5 cm ³
20	7.8 m	15.6 m	49.0 m	191.1 m ²	6.0 m	9.8 m	240.1 m ²	431.2 m ²	382.3 m ³

Aufgabe 4: Bestimme die fehlenden Größen (Radius r, Durchmesser d, Umfang u, Mantellinie s, Grundfläche G, Mantelfläche M, Oberfläche O, Volumen V) des Kegels.

Nr.	Gegeben:	Gesucht:
1	$d = 40.0 \text{ cm}, h = 29.4 \text{ cm}$	r, u, G, s, M, O, V
2	$d = 11.0 \text{ dm}, O = 378.4 \text{ dm}^2$	r, u, G, h, s, M, V
3	$u = 89.8 \text{ mm}, O = 1437.6 \text{ mm}^2$	r, d, G, h, s, M, V
4	$r = 14.9 \text{ mm}, V = 10741.0 \text{ mm}^3$	d, u, G, h, s, M, O
5	$d = 31.4 \text{ mm}, s = 39.0 \text{ mm}$	r, u, G, h, M, O, V
6	$G = 962.1 \text{ cm}^2, V = 6766.9 \text{ cm}^3$	r, d, u, h, s, M, O
7	$s = 28.0 \text{ cm}, M = 844.5 \text{ cm}^2$	r, d, u, G, h, O, V
8	$h = 26.1 \text{ m}, O = 556.3 \text{ m}^2$	r, d, u, G, s, M, V
9	$M = 2060.9 \text{ dm}^2, V = 10280.4 \text{ dm}^3$	r, d, u, G, h, s, O
10	$u = 65.3 \text{ dm}, M = 911.6 \text{ dm}^2$	r, d, G, h, s, O, V
11	$h = 15.1 \text{ dm}, M = 365.1 \text{ dm}^2$	r, d, u, G, s, O, V
12	$u = 79.2 \text{ cm}, s = 35.1 \text{ cm}$	r, d, G, h, M, O, V
13	$G = 897.3 \text{ mm}^2, M = 1290.2 \text{ mm}^2$	r, d, u, h, s, O, V
14	$r = 12.8 \text{ m}, O = 1930.2 \text{ m}^2$	d, u, G, h, s, M, V

15	$r = 6.5 \text{ m}, M = 663.7 \text{ m}^2$	d, u, G, h, s, O, V
16	$s = 19.9 \text{ dm}, M = 719.0 \text{ dm}^2$	r, d, u, G, h, O, V
17	$M = 1501.6 \text{ mm}^2, V = 6412.4 \text{ mm}^3$	r, d, u, G, h, s, O
18	$r = 11.8 \text{ mm}, s = 29.0 \text{ mm}$	d, u, G, h, M, O, V
19	$s = 21.4 \text{ dm}, M = 1109.3 \text{ dm}^2$	r, d, u, G, h, O, V
20	$G = 227.0 \text{ cm}^2, O = 1439.3 \text{ cm}^2$	r, d, u, h, s, M, V

Vorgehensweise: Zur Ermittlung der fehlenden Größen beim Kegel ist die obige Formelsammlung anzuwenden.

Lösungen:

Nr.	r=	d=	u=	G=	h=	s=	M=	O=	V=
1	20.0 cm	40.0 cm	125.7 cm	1256.6 cm ²	29.4 cm	35.6 cm	2236.8 cm ²	3493.4 cm ²	12315.0 cm ³
2	5.5 dm	11.0 dm	34.6 dm	95.0 dm ²	15.5 dm	16.4 dm	283.4 dm ²	378.4 dm ²	491.0 dm ³
3	14.3 mm	28.6 mm	89.8 mm	642.4 mm ²	10.4 mm	17.7 mm	795.2 mm ²	1437.6 mm ²	2227.1 mm ³
4	14.9 mm	29.8 mm	93.6 mm	697.5 mm ²	46.2 mm	48.5 mm	2270.3 mm ²	2967.8 mm ²	10741.0 mm ³
5	15.7 mm	31.4 mm	98.6 mm	774.4 mm ²	35.7 mm	39.0 mm	1923.6 mm ²	2698.0 mm ²	9215.0 mm ³
6	17.5 cm	35.0 cm	110.0 cm	962.1 cm ²	21.1 cm	27.4 cm	1506.4 cm ²	2468.5 cm ²	6766.9 cm ³
7	9.6 cm	19.2 cm	60.3 cm	289.5 cm ²	26.3 cm	28.0 cm	844.5 cm ²	1134.0 cm ²	2538.2 cm ³
8	5.5 m	11.0 m	34.6 m	95.0 m ²	26.1 m	26.7 m	461.3 m ²	556.3 m ²	826.8 m ³
9	16.4 dm	32.8 dm	103.0 dm	845.0 dm ²	36.5 dm	40.0 dm	2060.9 dm ²	2905.9 dm ²	10280.4 dm ³
10	10.4 dm	20.8 dm	65.3 dm	339.8 dm ²	25.9 dm	27.9 dm	911.6 dm ²	1251.4 dm ²	2933.6 dm ³
11	7.0 dm	14.0 dm	44.0 dm	153.9 dm ²	15.1 dm	16.6 dm	365.1 dm ²	519.0 dm ²	774.8 dm ³
12	12.6 cm	25.2 cm	79.2 cm	498.8 cm ²	32.8 cm	35.1 cm	1389.4 cm ²	1888.2 cm ²	5453.1 cm ³
13	16.9 mm	33.8 mm	106.2 mm	897.3 mm ²	17.5 mm	24.3 mm	1290.2 mm ²	2187.5 mm ²	5234.1 mm ³
14	12.8 m	25.6 m	80.4 m	514.7 m ²	32.8 m	35.2 m	1415.5 m ²	1930.2 m ²	5627.6 m ³
15	6.5 m	13.0 m	40.8 m	132.7 m ²	31.8 m	32.5 m	663.7 m ²	796.4 m ²	1407.0 m ³
16	11.5 dm	23.0 dm	72.3 dm	415.5 dm ²	16.3 dm	19.9 dm	719.0 dm ²	1134.5 dm ²	2257.4 dm ³
17	14.1 mm	28.2 mm	88.6 mm	624.6 mm ²	30.8 mm	33.9 mm	1501.6 mm ²	2126.2 mm ²	6412.4 mm ³
18	11.8 mm	23.6 mm	74.1 mm	437.4 mm ²	26.5 mm	29.0 mm	1075.1 mm ²	1512.5 mm ²	3864.0 mm ³
19	16.5 dm	33.0 dm	103.7 dm	855.3 dm ²	13.6 dm	21.4 dm	1109.3 dm ²	1964.6 dm ²	3877.4 dm ³
20	8.5 cm	17.0 cm	53.4 cm	227.0 cm ²	44.6 cm	45.4 cm	1212.3 cm ²	1439.3 cm ²	3374.4 cm ³

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